



# Racetrack FFAG muon decay ring for vSTORM

JB. Lagrange, J. Pasternak, Y. Mori



# Outline





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## ● Zero-chromatic FFAG



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- Zero-chromatic FFAG
- Racetrack FFAG muon decay ring



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- Comparison



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● Zero-chromatic FFAG

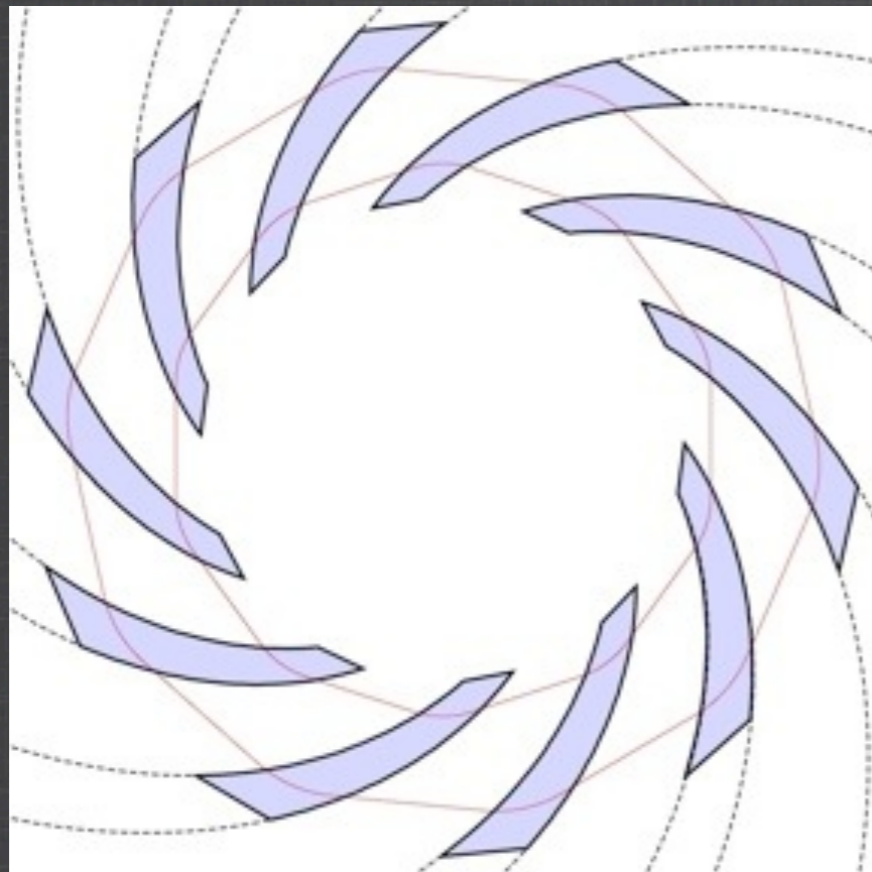
● Racetrack FFAG muon decay ring

● Comparison

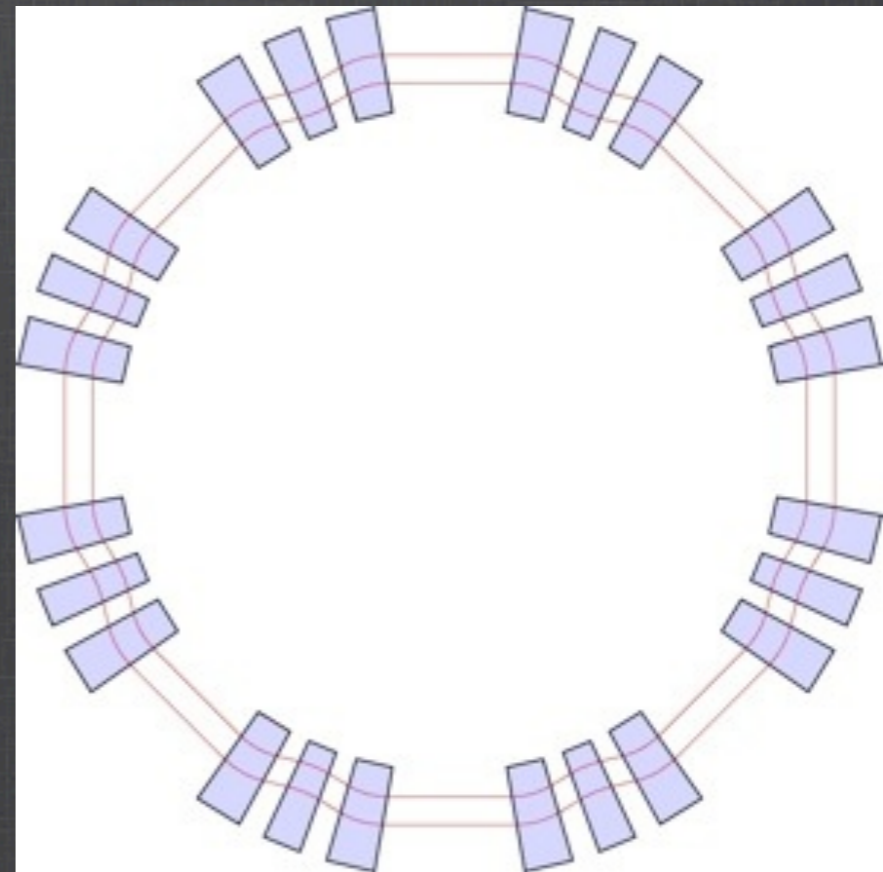
# Circular scaling FFAG

Geometrical field index:  $k = \frac{R}{\bar{B}} \frac{d\bar{B}}{dR}$

$$B(r, \theta) = B_0 \left( \frac{r}{r_0} \right)^k \cdot \mathcal{F}\left(\theta - \tan \zeta \ln \frac{r}{r_0}\right)$$



Spiral sector

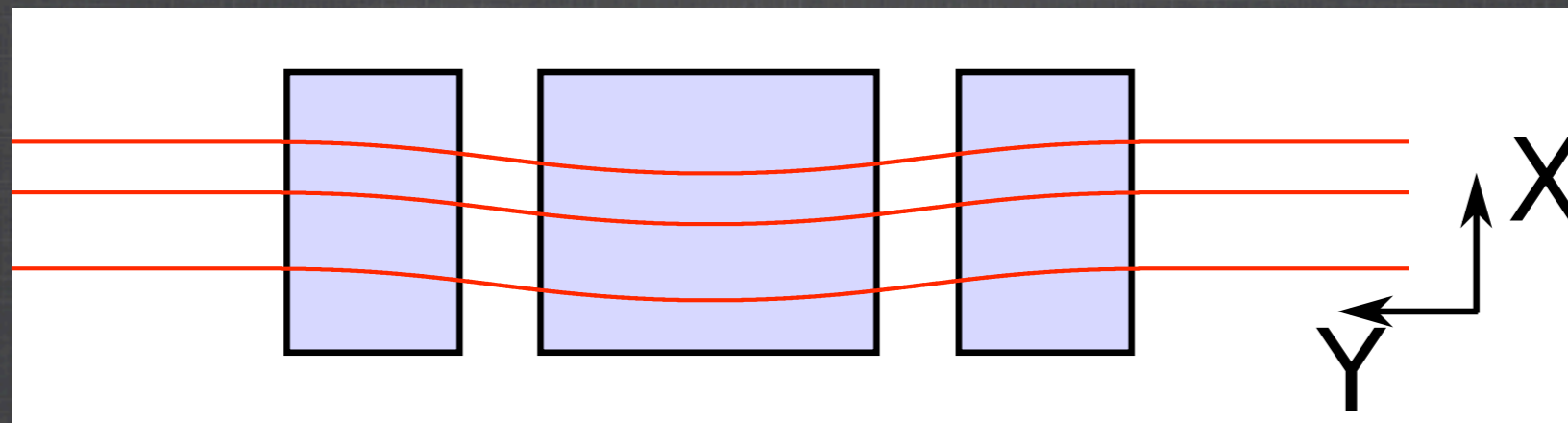


Radial sector

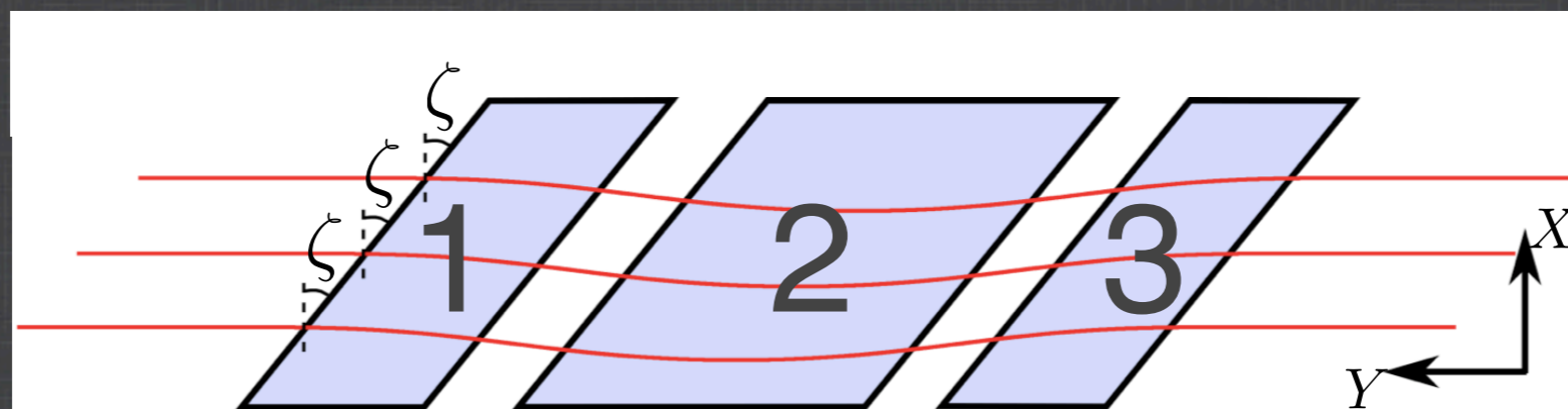
# Straight scaling FFAG

Normalized field gradient:  $m = \frac{1}{\bar{B}} \frac{d\bar{B}}{d\chi}$

$$B(X, Y) = B_0 e^{m(X-X_0)} \mathcal{F}(Y - (X - X_0) \tan \zeta)$$



Rectangular case

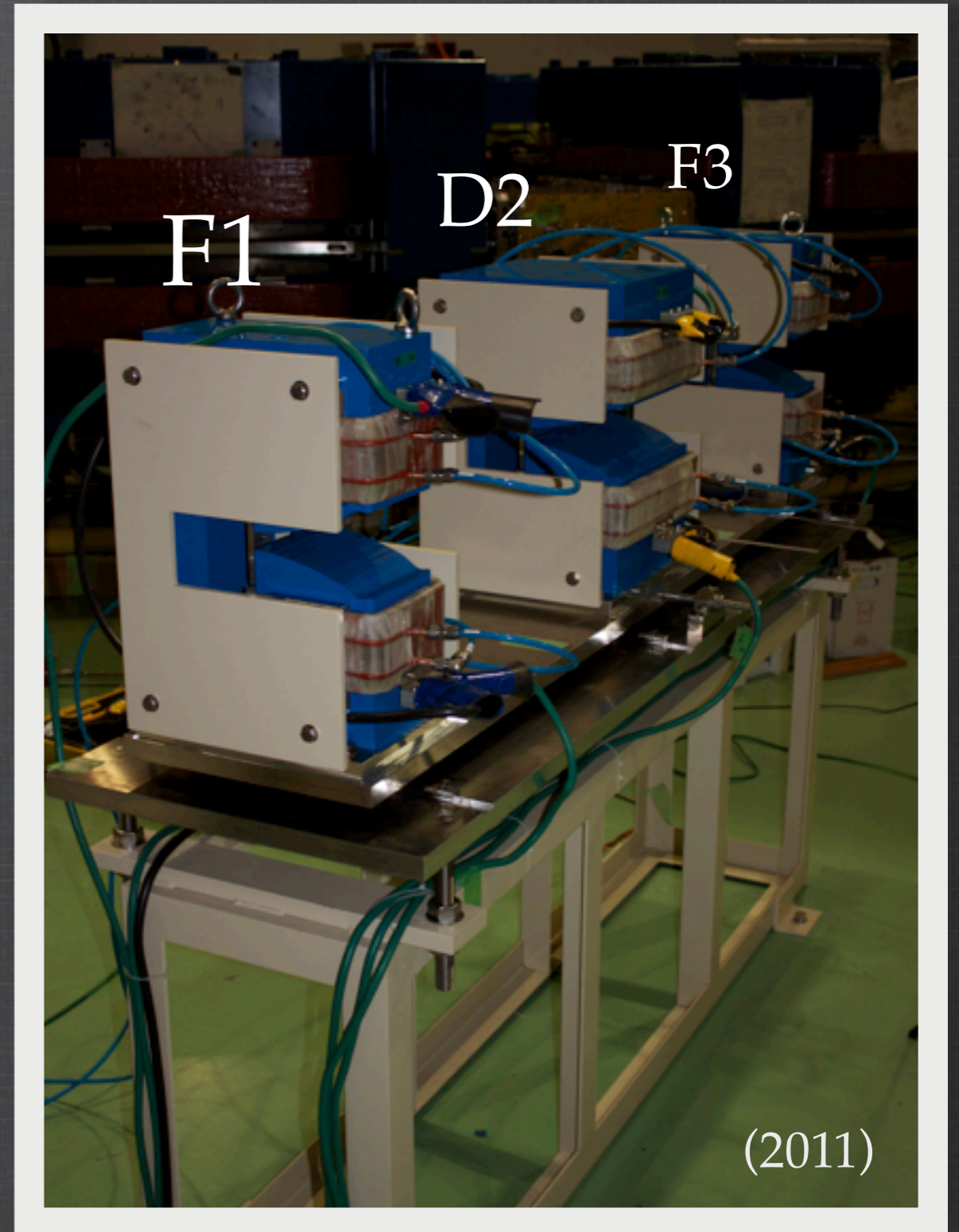
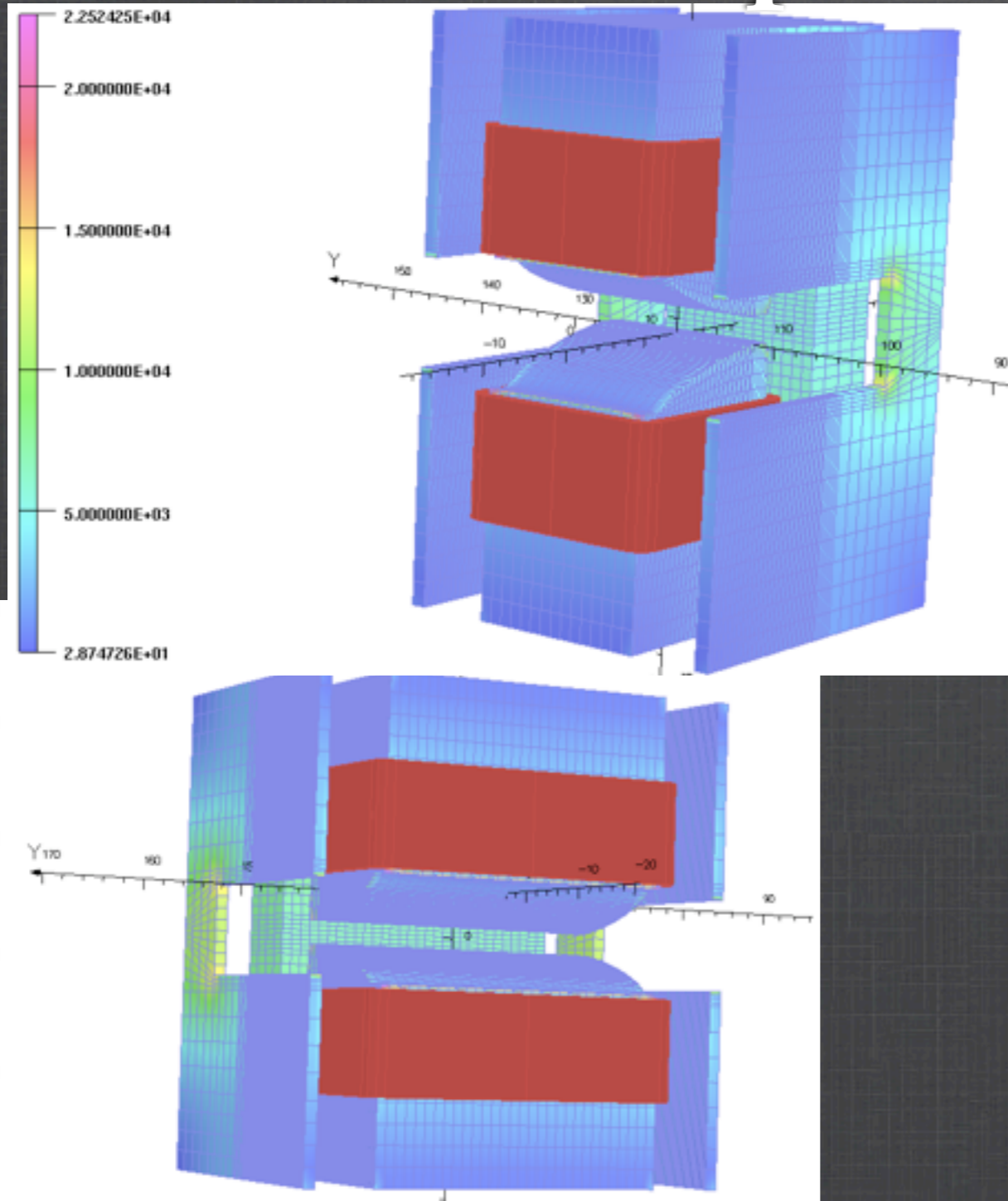


Tilted straight case





# Straight scaling FFAG experiment



(2011)

JB. Lagrange *et al.*, Straight scaling FFAG beam line,  
*NIM A*, vol. 691, pp. 55-63, ISSN 0168-9002 (2012).



# Outline



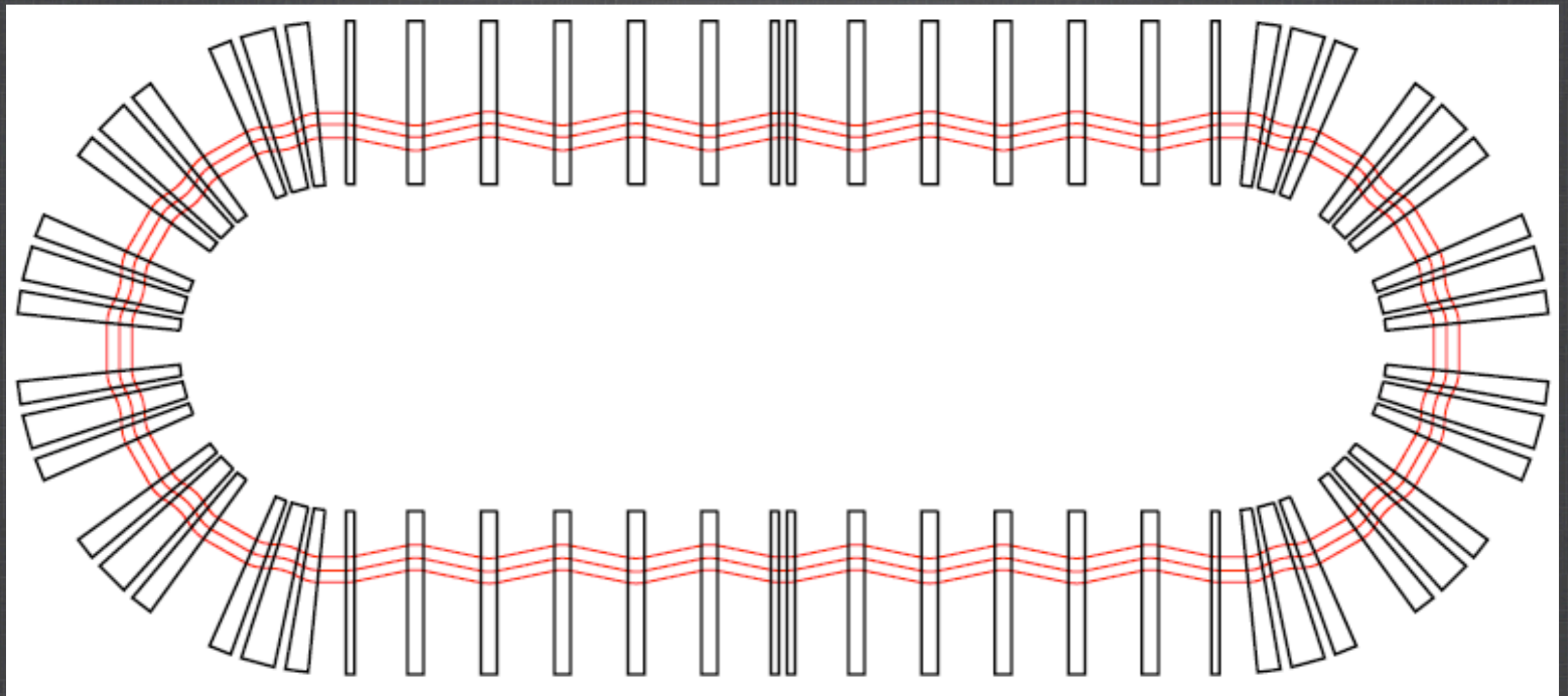
- Zero-chromatic FFAG

- Racetrack FFAG muon decay ring

- Comparison



# Racetrack FFAG





# vSTORM Racetrack FFAG





# vSTORM Racetrack FFAG



Constraints:

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- in the dispersion matching section, a drift length of  $\sim 2.6$  m is necessary for stochastic injection.
- to keep the ring as small as possible, SC magnets (super-ferric, up to 3 T) in the arcs are considered. Normal conducting magnets are used in the straight part.

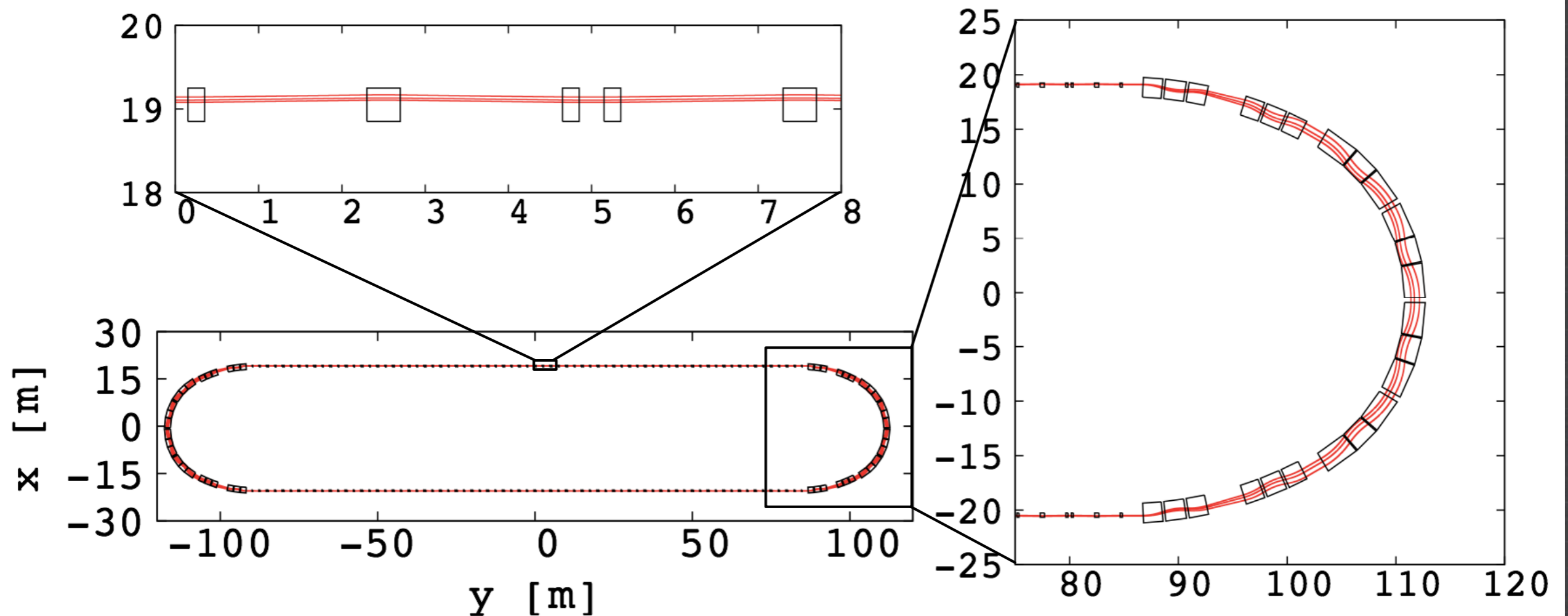


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- in the dispersion matching section, a drift length of  $\sim 2.6$  m is necessary for stochastic injection.
- to keep the ring as small as possible, SC magnets (super-ferric, up to 3 T) in the arcs are considered. Normal conducting magnets are used in the straight part.
- large transverse acceptance is needed in both planes ( $1000\pi$  mm.mrad).

# OPTION #1: "FODO-LIKE"

Straight: 175 m, maximum scallop angle: 12 mrad



Comparable straight length than FODO lattice



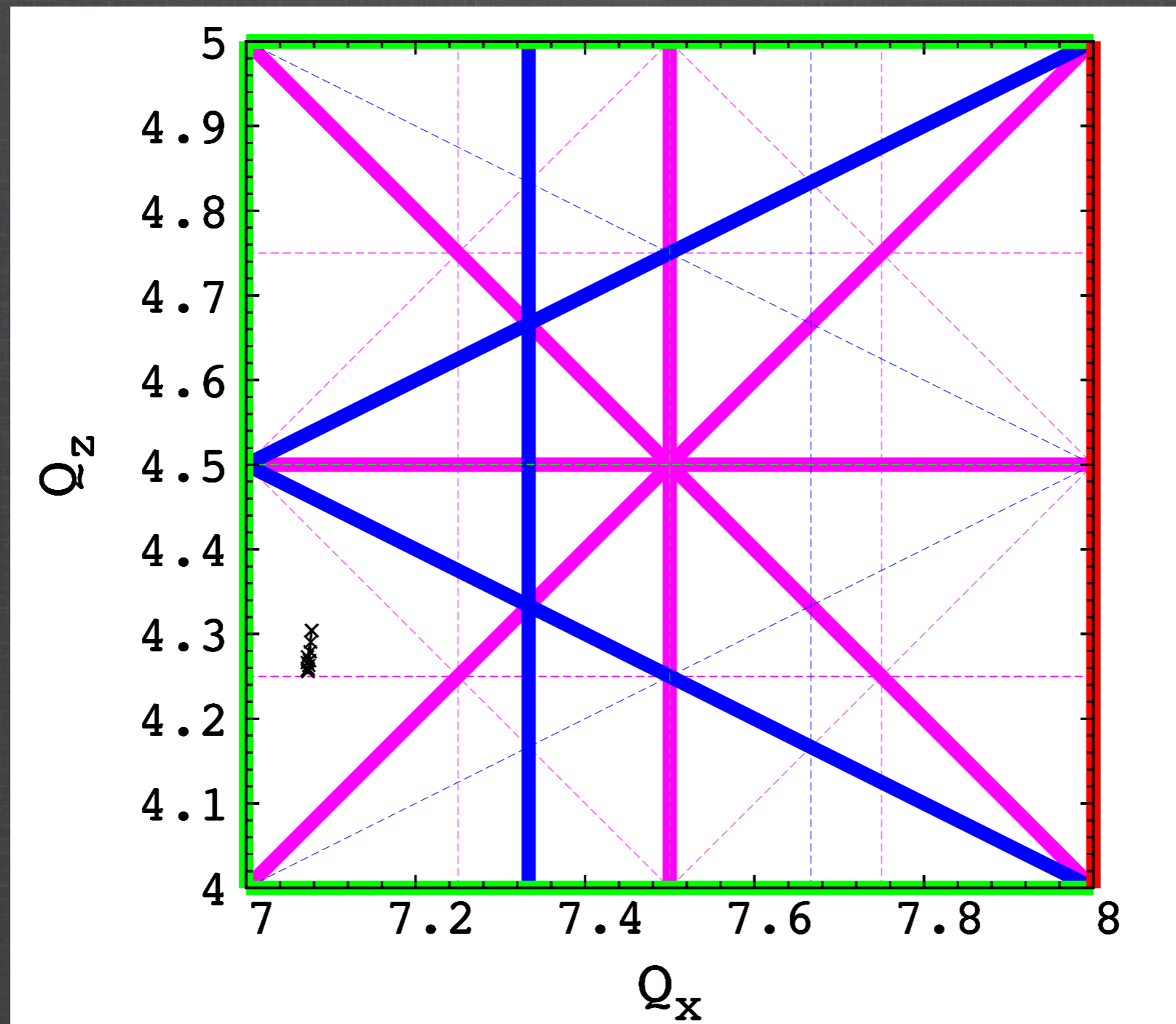
# OPTION #1: “FODO-LIKE”

## Cell parameters

|                                      | Circular<br>Section | Matching<br>Section | Straight<br>Section |
|--------------------------------------|---------------------|---------------------|---------------------|
| Type                                 | FDF                 | FDF                 | DFD                 |
| Cell radius/length [m]               | 17.3                | 36.1                | 5                   |
| Opening angle [deg]                  | 30                  | 15                  |                     |
| k-value/m-value                      | 6.202               | 26.785              | 5 m <sup>-1</sup>   |
| Packing factor                       | 0.92                | 0.58                | 0.16                |
| Horizontal phase advance /cell [deg] | 90.0                | 90.0                | 15.8                |
| Vertical phase advance /cell [deg]   | 21.1                | 23.7                | 16.8                |
| Average dispersion /cell [m]         | 2.4                 | 1.3                 | 0.2                 |
| Number of cells /ring                | 4 × 2               | 4 × 2               | 35 × 2              |

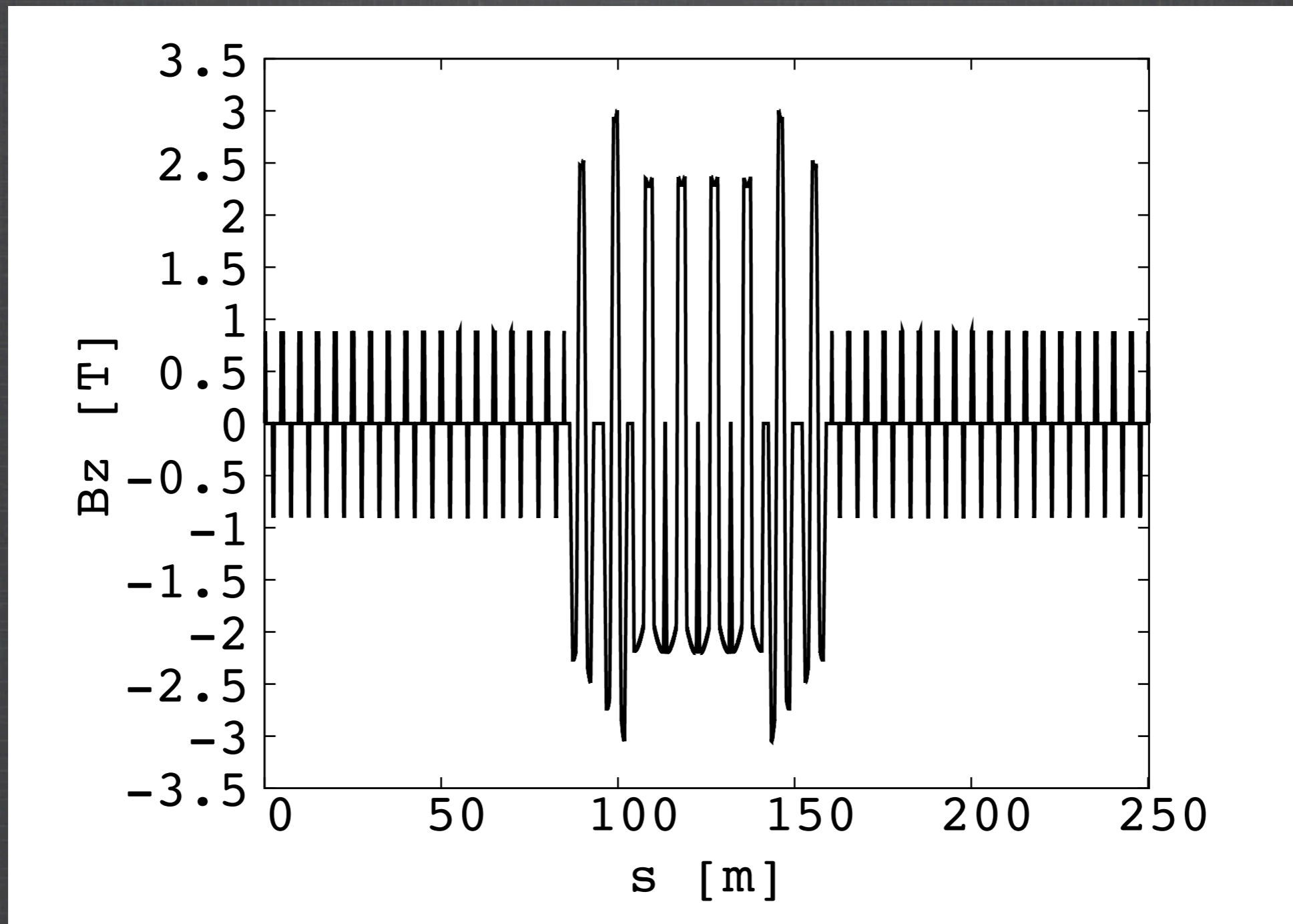
# OPTION #1

Tune diagram  $\frac{\Delta P}{P} = \pm 16\%$



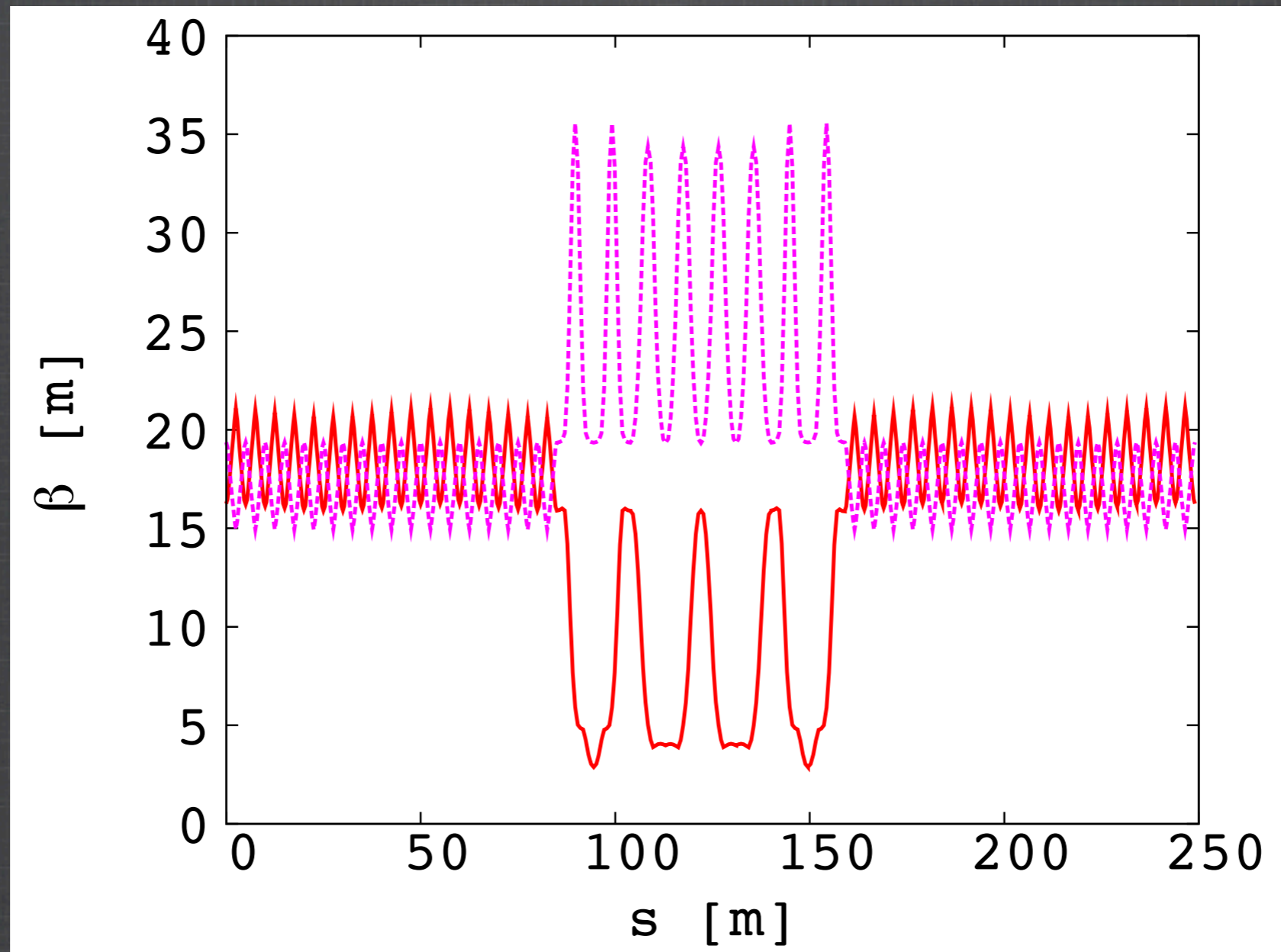
# OPTION #1

Magnetic field for  $P_{\max}$  (+16%)



# OPTION #1

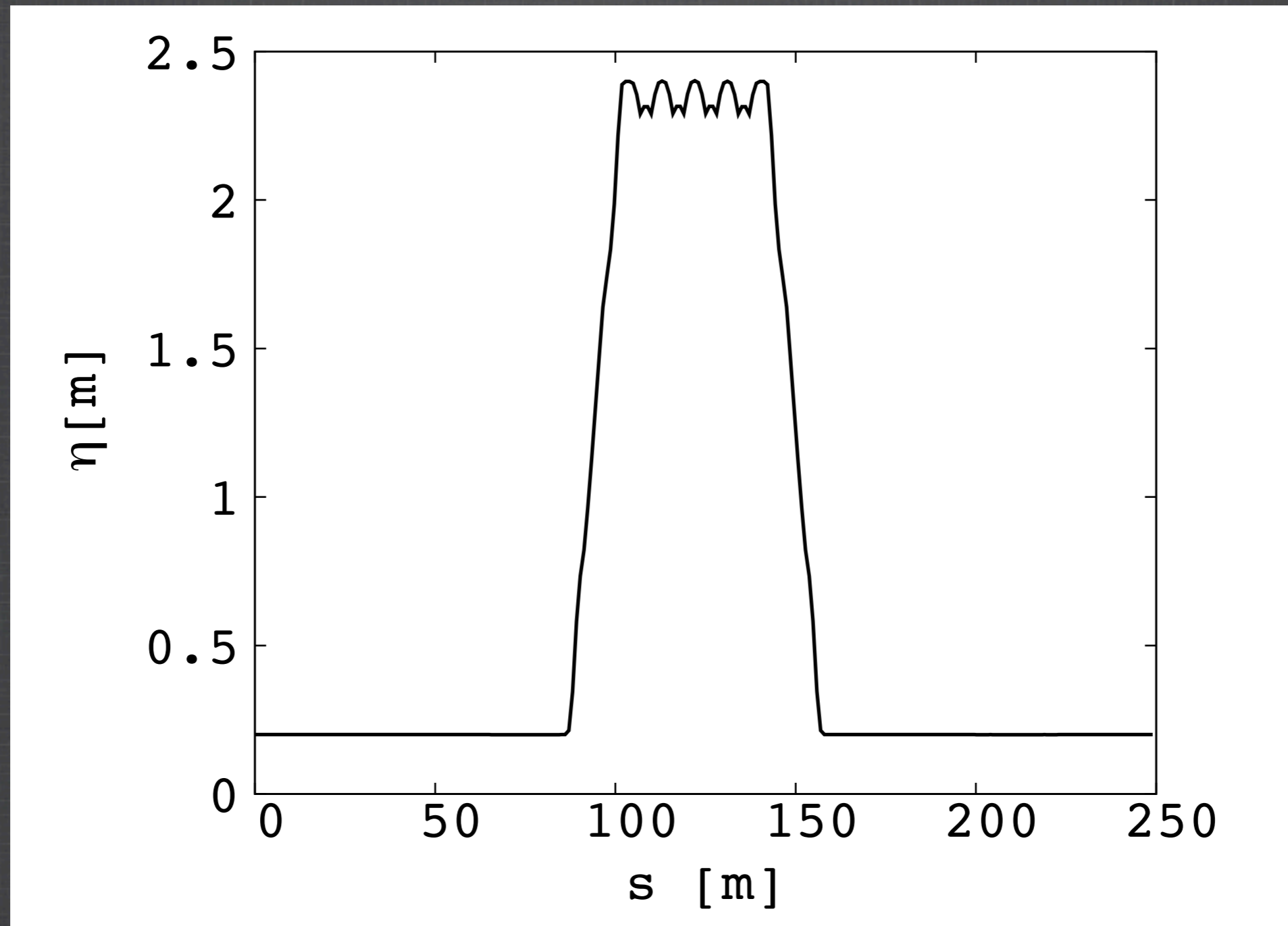
## Beta-functions at matching momentum



Horizontal (plain red) and vertical (dotted purple) betafunctions for half of the ring.

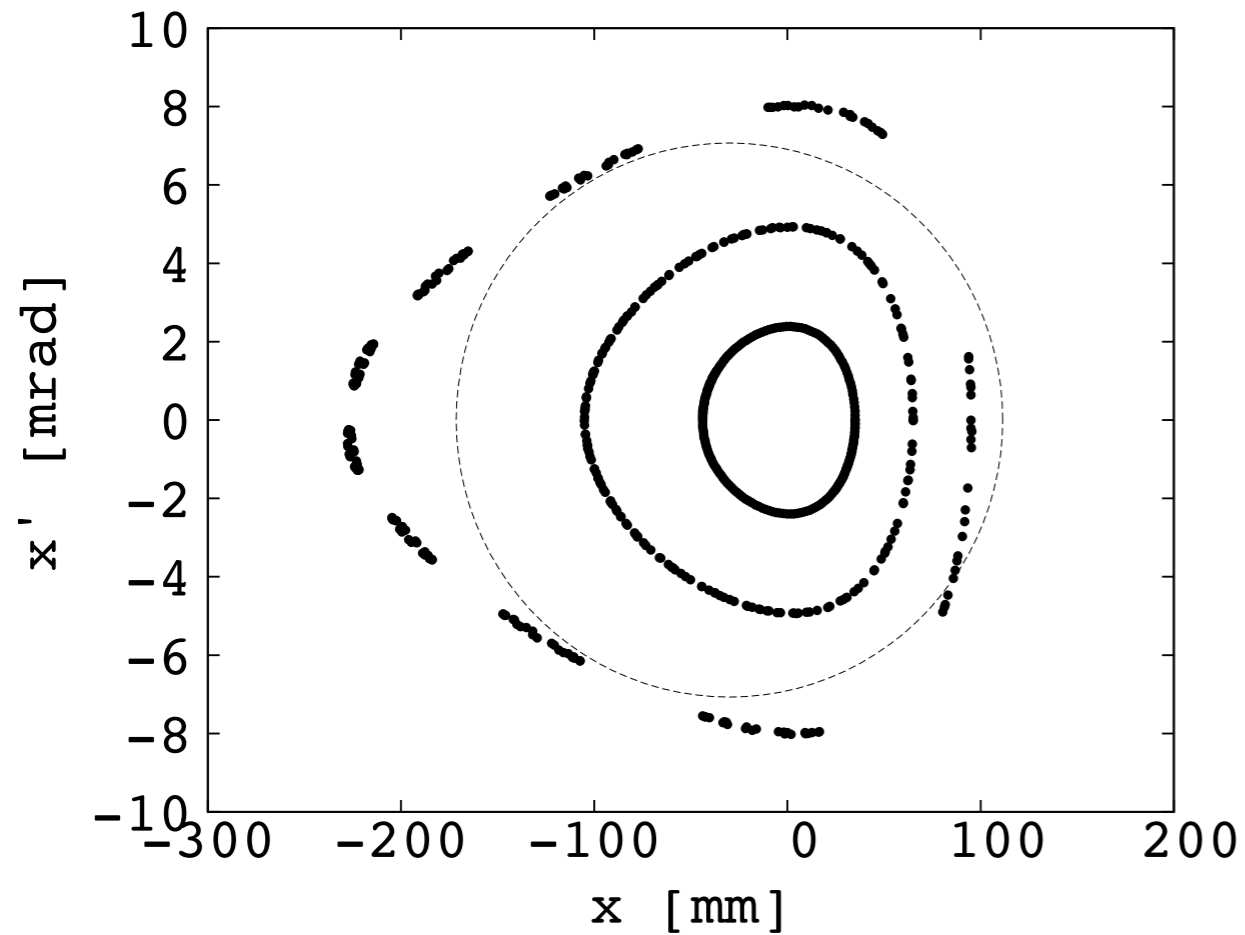
# OPTION #1

## Dispersion function at matching momentum

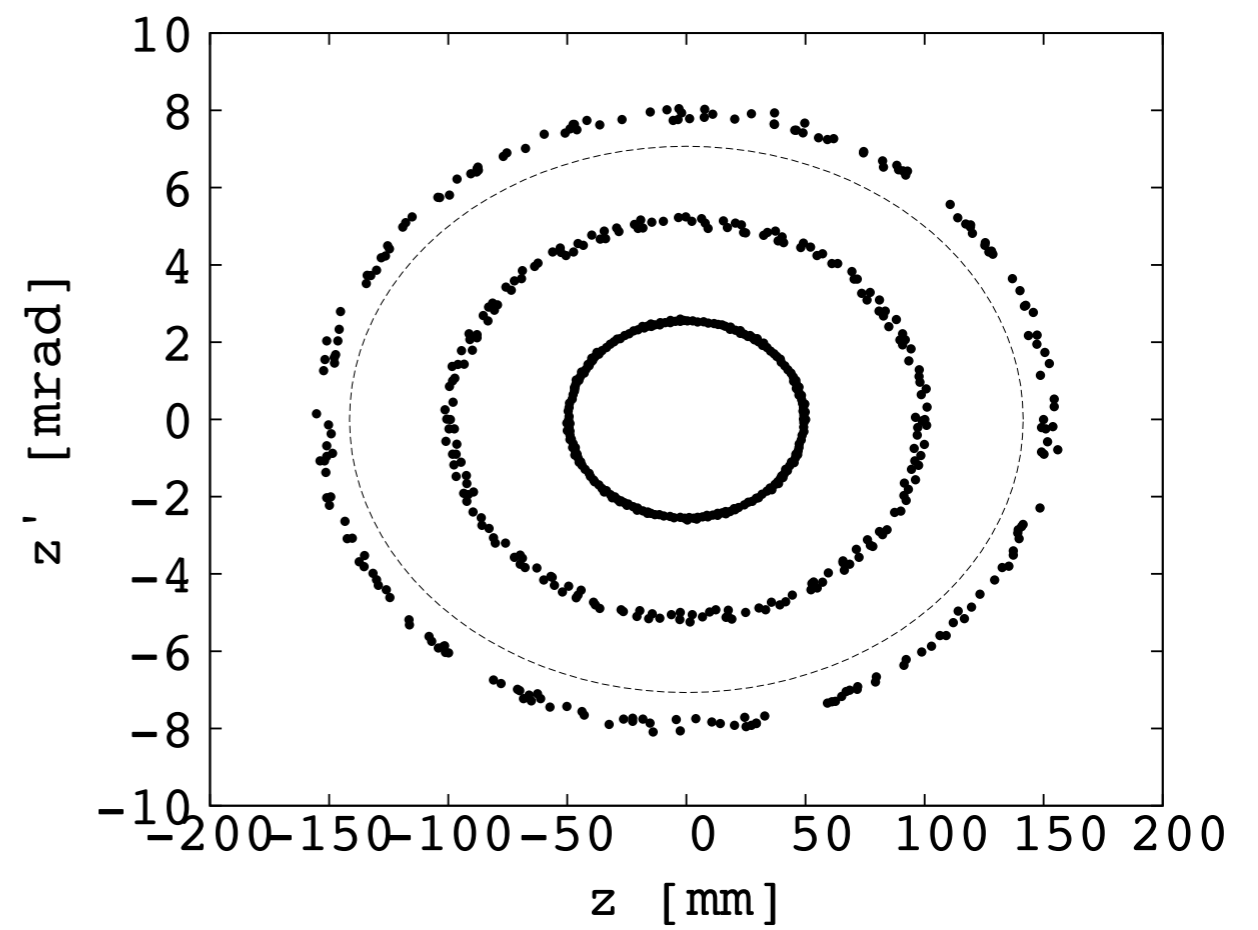


# OPTION #1

## Transverse acceptance



Maximum horizontal stable amplitude over 100 turns

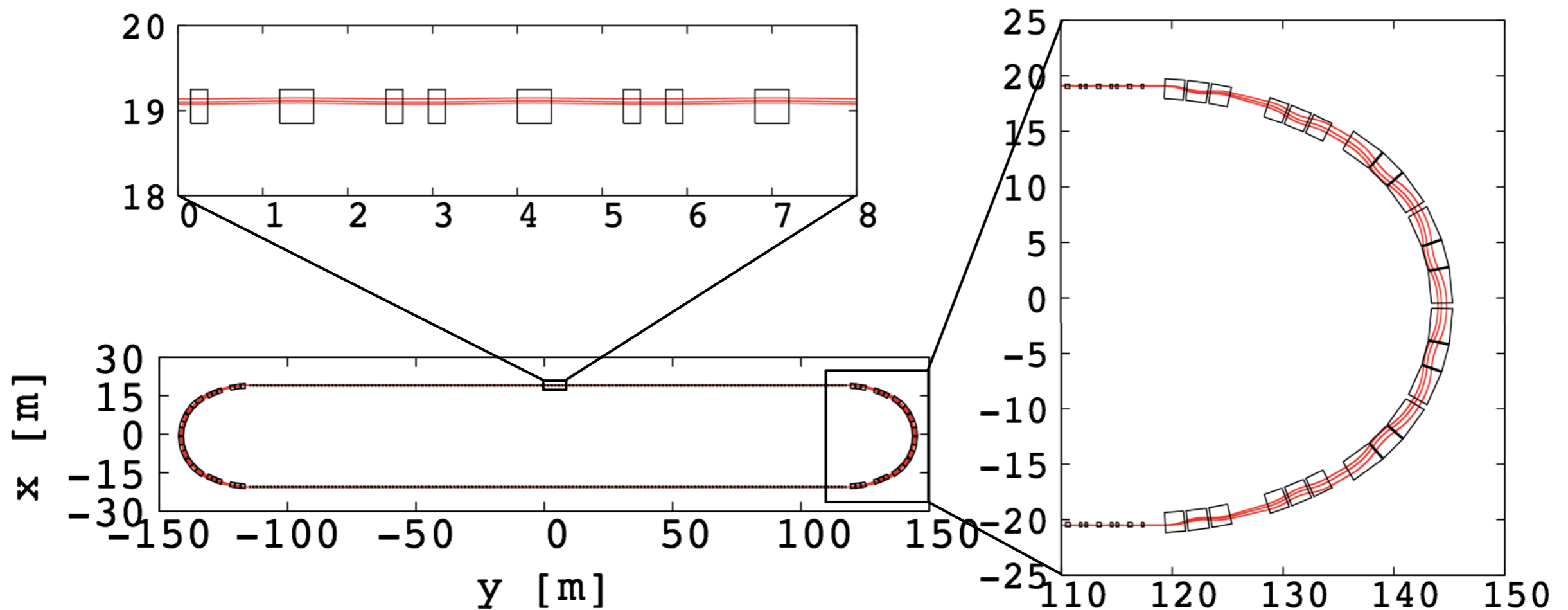


Maximum vertical stable amplitude over 100 turns



# OPTION #2: "LONG"

Straight: 230 m, maximum scallop angle: 12.5 mrad



Long straight length for a greater number of decayed pions.



# OPTION #2: "LONG"

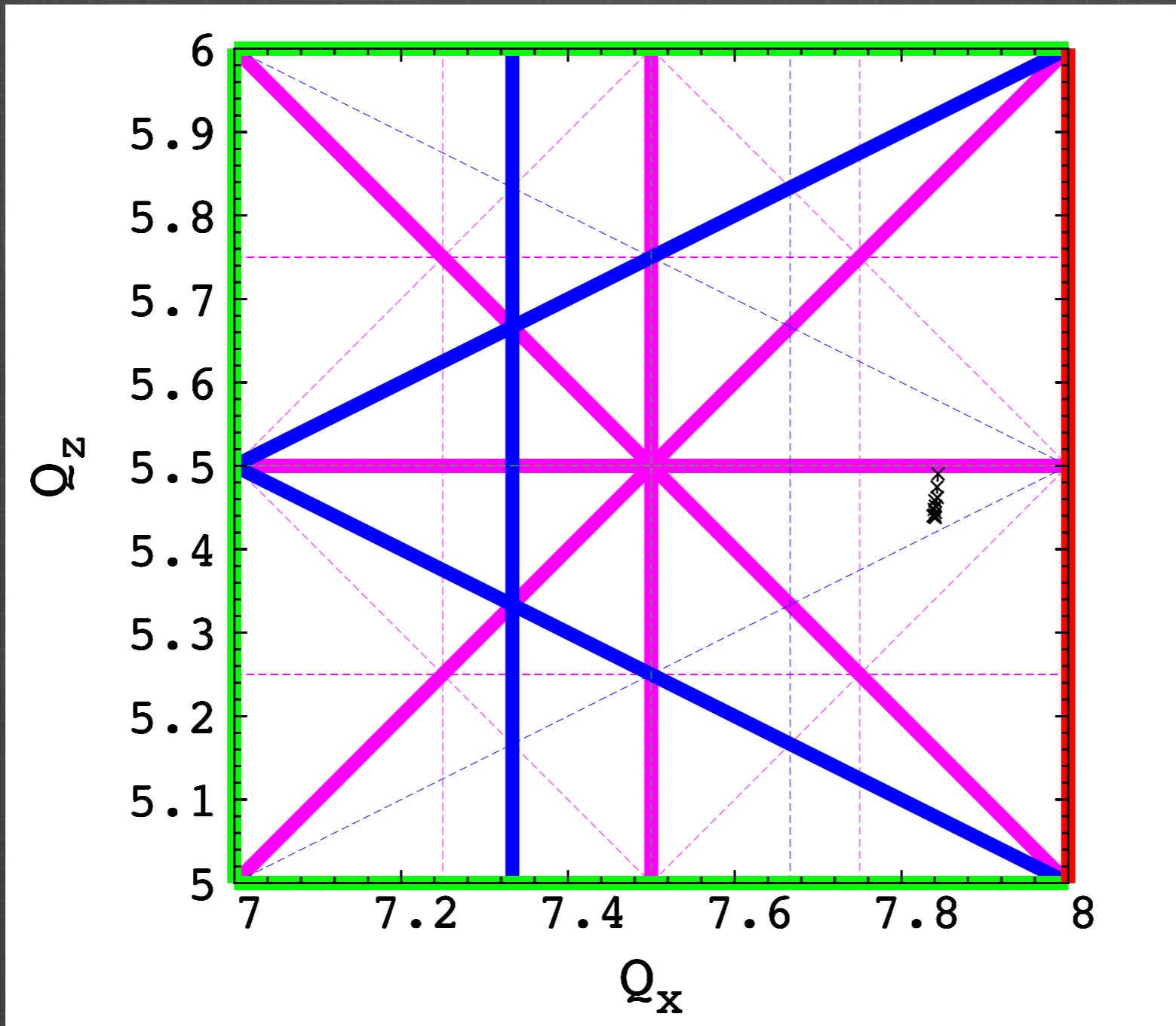


## Cell parameters

|                                      | Circular Section | Matching Section | Straight Section  |
|--------------------------------------|------------------|------------------|-------------------|
| Type                                 | FDF              | FDF              | DFD               |
| Cell radius/length [m]               | 17.3             | 36.1             | 2.8               |
| Opening angle [deg]                  | 30               | 15               |                   |
| k-value/m-value                      | 6.19             | 26.72            | 5 m <sup>-1</sup> |
| Packing factor                       | 0.92             | 0.58             | 0.29              |
| Horizontal phase advance /cell [deg] | 90.0             | 90.0             | 8.3               |
| Vertical phase advance /cell [deg]   | 22.6             | 25.5             | 9.5               |
| Average dispersion /cell [m]         | 2.4              | 1.3              | 0.2               |
| Number of cells /ring                | 4 × 2            | 4 × 2            | 83 × 2            |

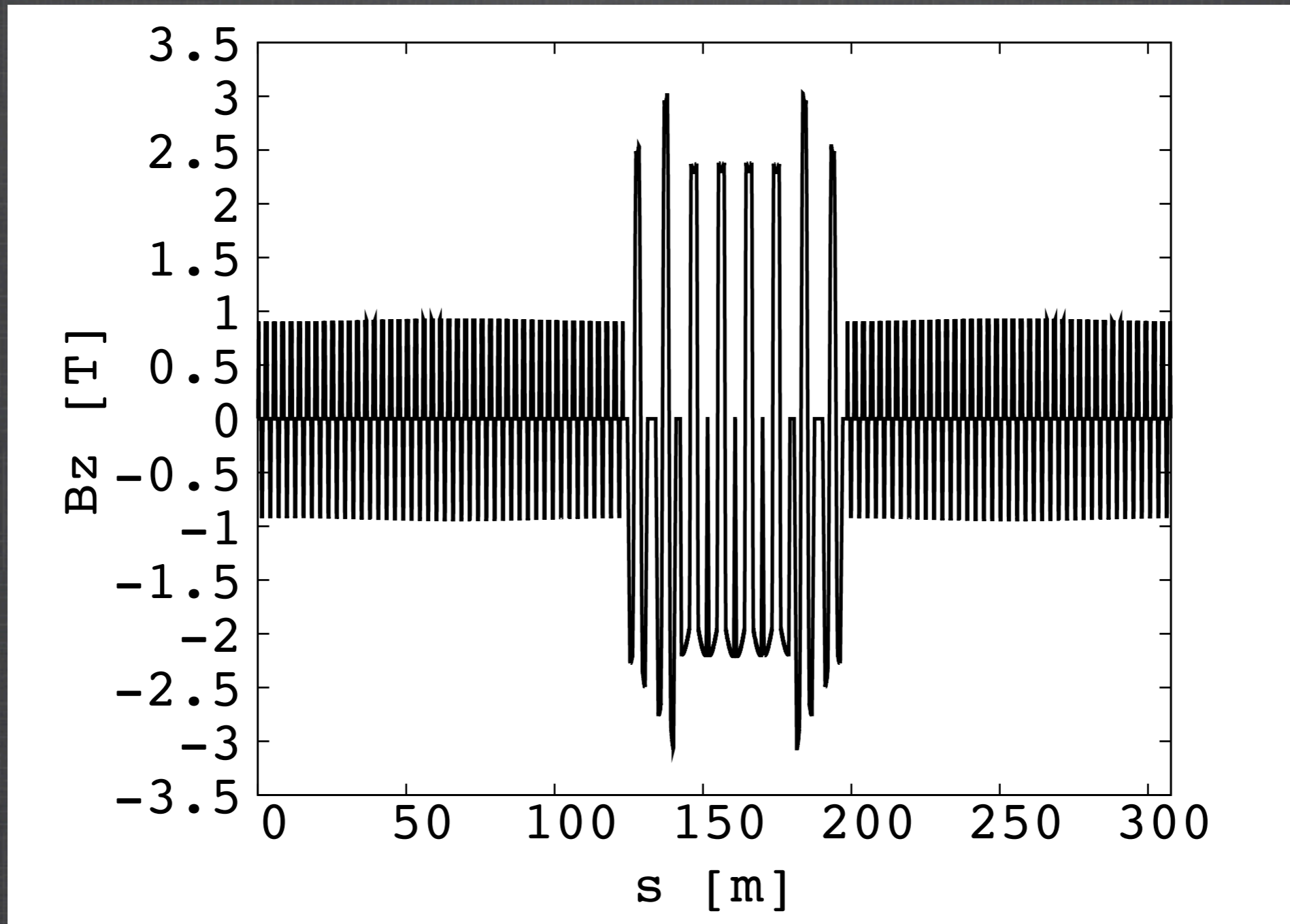
# OPTION #2

Tune diagram  $\frac{\Delta P}{P} = \pm 16\%$



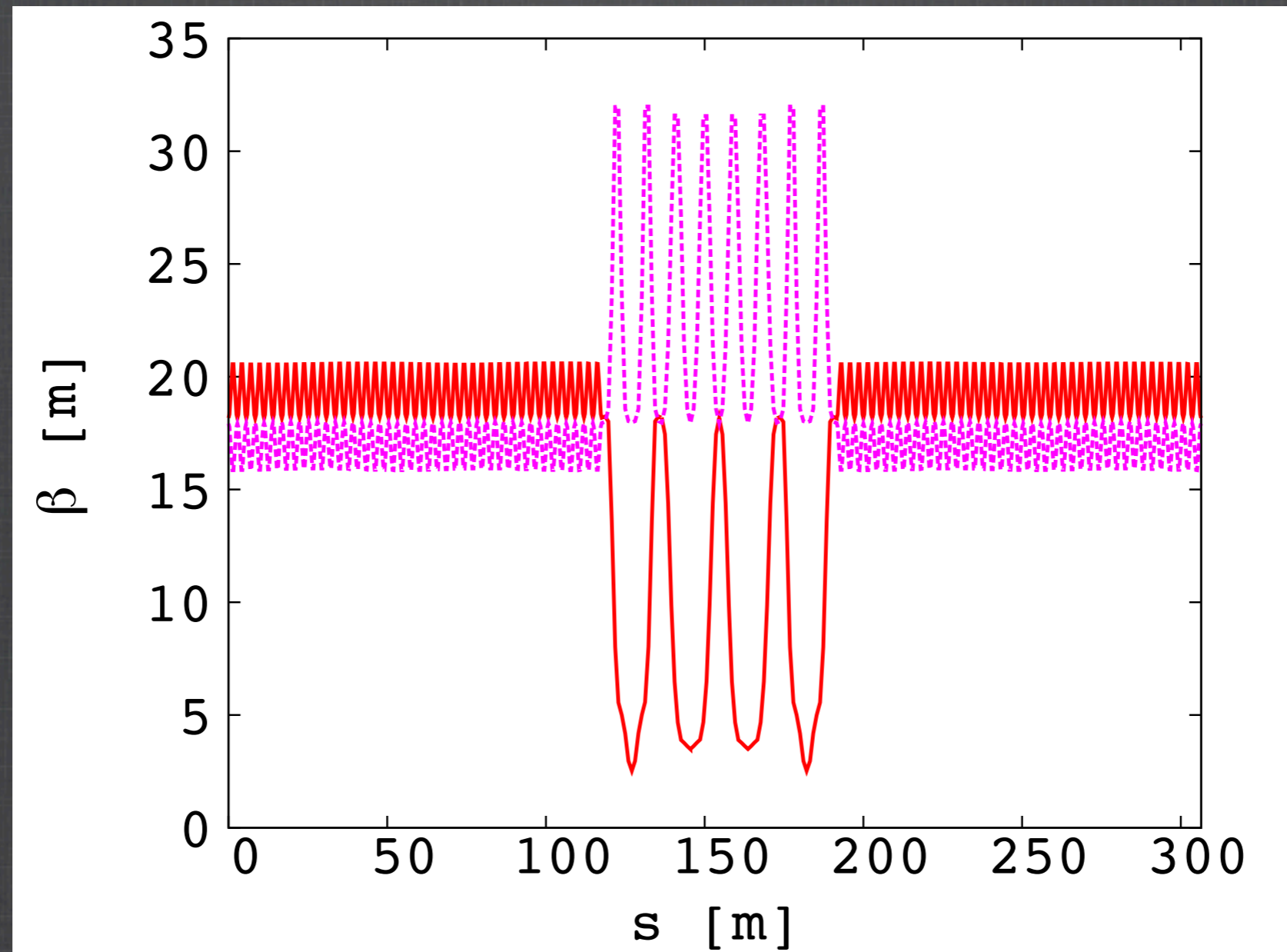
# OPTION #2

Magnetic field for  $P_{\max}$  (+16%)



# OPTION #2

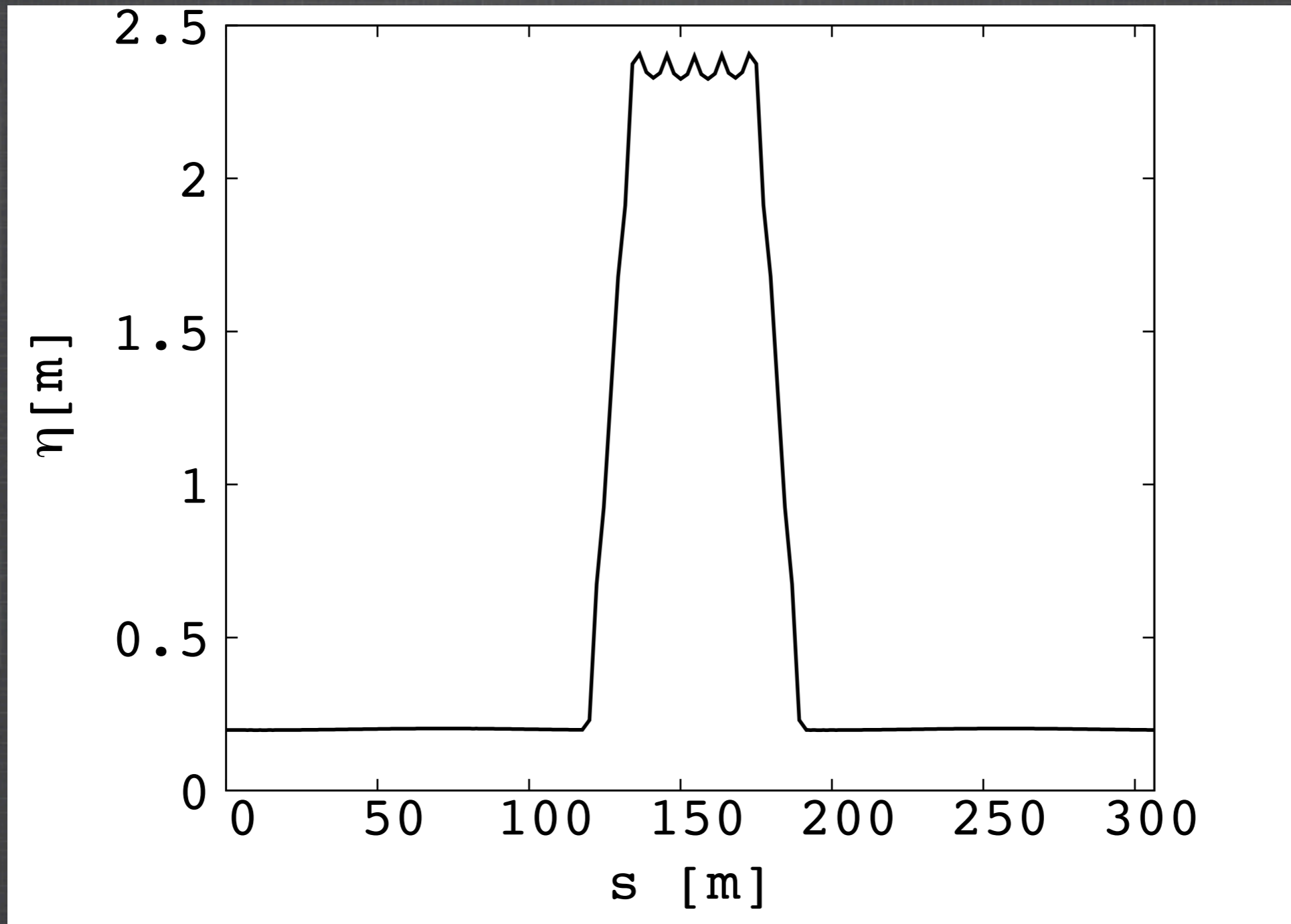
## Beta-functions at matching momentum



Horizontal (plain red) and vertical (dotted purple) betafunctions for half of the ring.

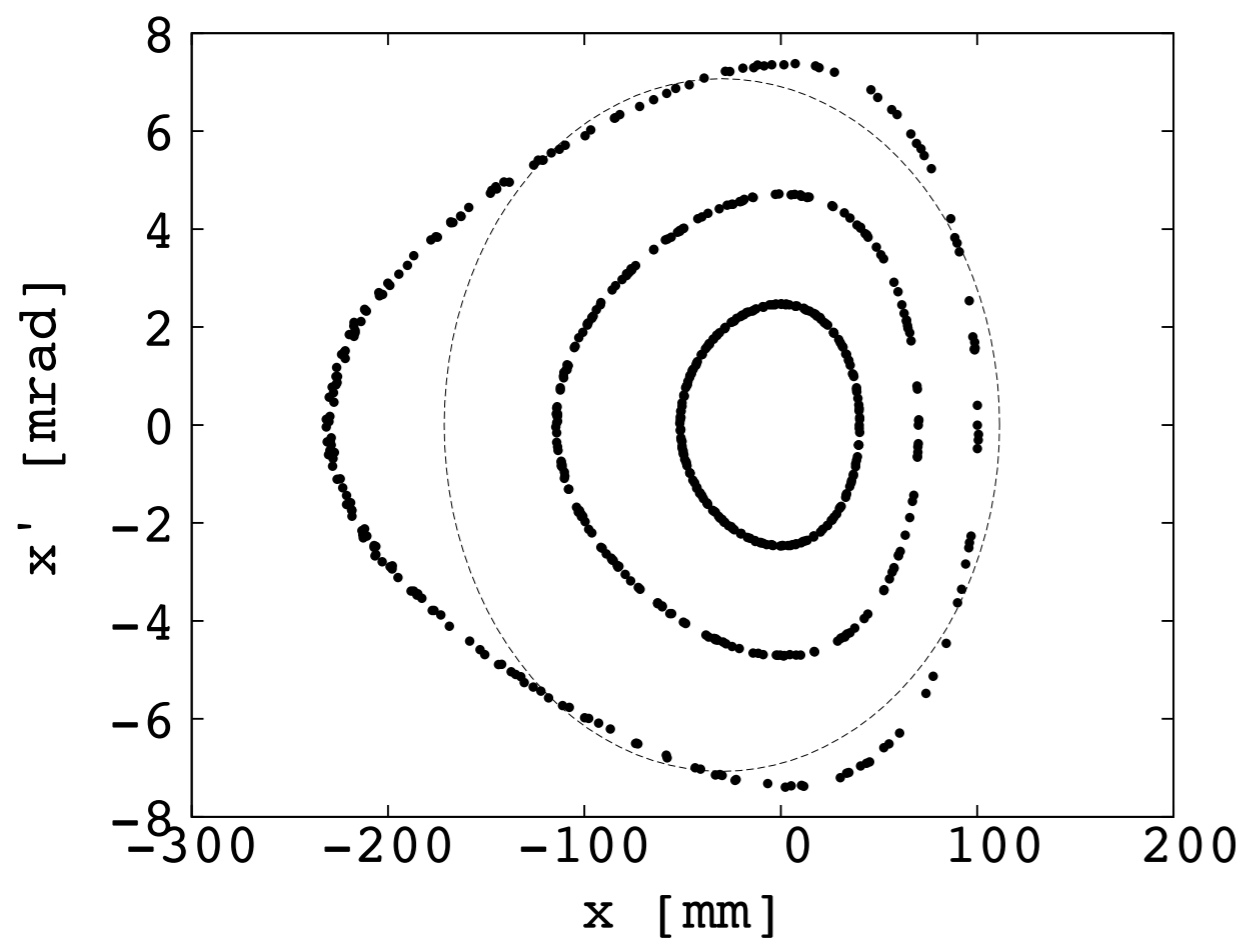
# OPTION #2

## Dispersion function at matching momentum

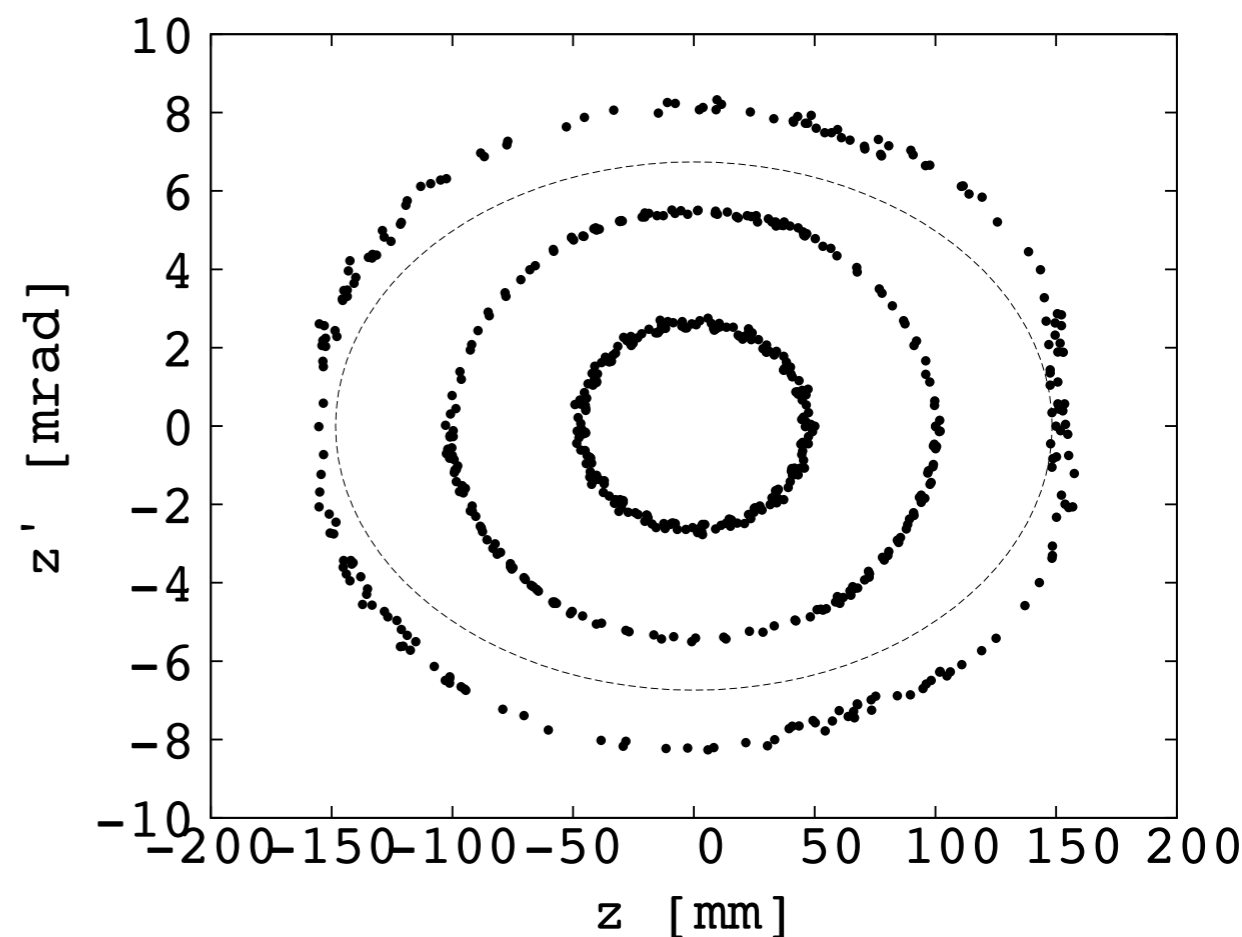


# OPTION #2

## Transverse acceptance



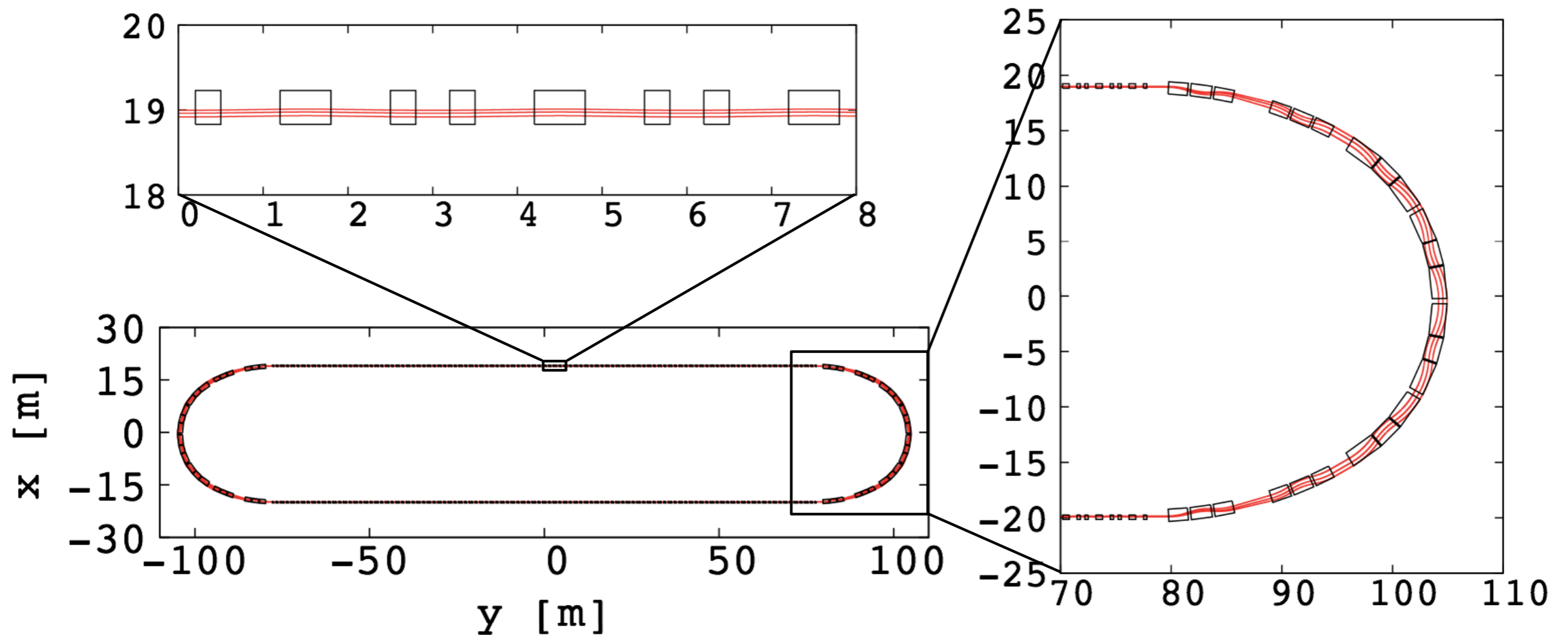
Maximum horizontal stable amplitude over 100 turns



Maximum vertical stable amplitude over 100 turns

# OPTION #3: "LOW-COST"

Straight: 156 m, maximum scallop angle: 13.9 mrad



Short straight length for a cheaper lattice.





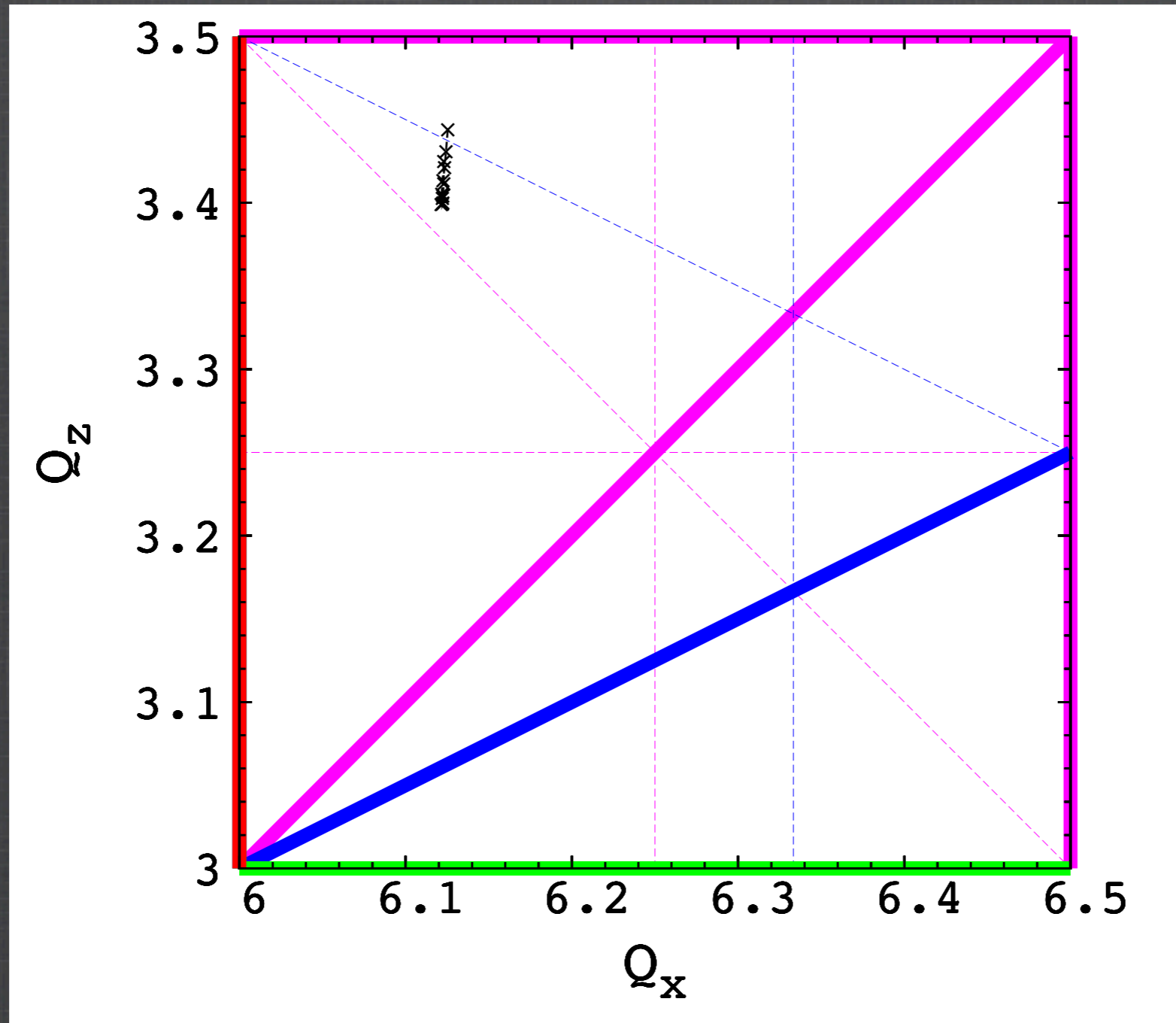
# OPTION #3: “LOW-COST”

## Cell parameters

|                                      | Circular<br>Section | Matching<br>Section | Straight<br>Section |
|--------------------------------------|---------------------|---------------------|---------------------|
| Type                                 | FDF                 | FDF                 | DFD                 |
| Cell radius/length [m]               | 17                  | 36.15               | 3                   |
| Opening angle [deg]                  | 30                  | 15                  |                     |
| k-value/m-value                      | 6.21                | 26.83               | $4 \text{ m}^{-1}$  |
| Packing factor                       | 0.92                | 0.58                | 0.4                 |
| Horizontal phase advance /cell [deg] | 90.0                | 90.0                | 7.3                 |
| Vertical phase advance /cell [deg]   | 19.1                | 21.9                | 8.6                 |
| Average dispersion /cell [m]         | 2.4                 | 1.3                 | 0.25                |
| Number of cells /ring                | $4 \times 2$        | $4 \times 2$        | $52 \times 2$       |

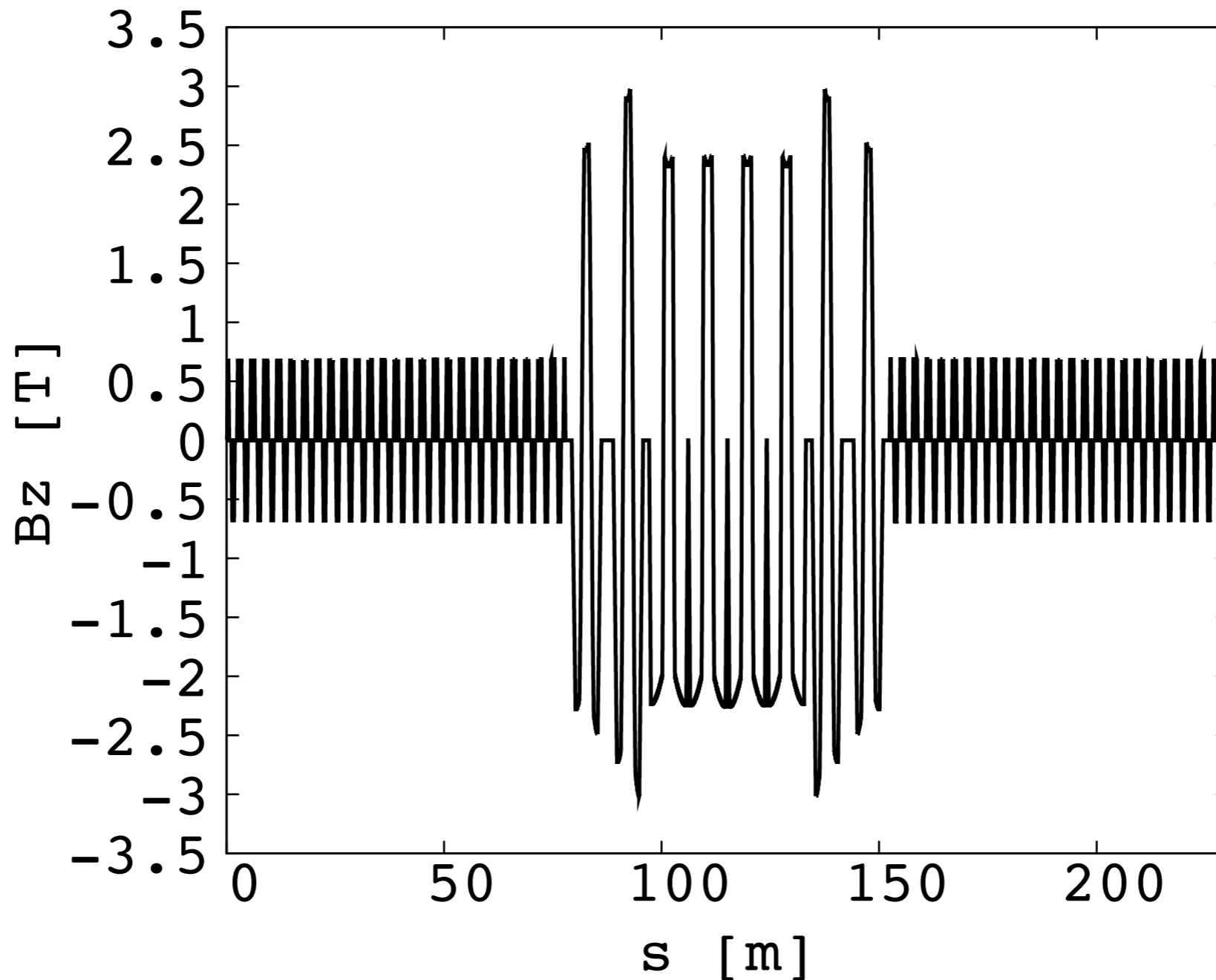
# OPTION #3

Tune diagram  $\frac{\Delta P}{P} = \pm 16\%$



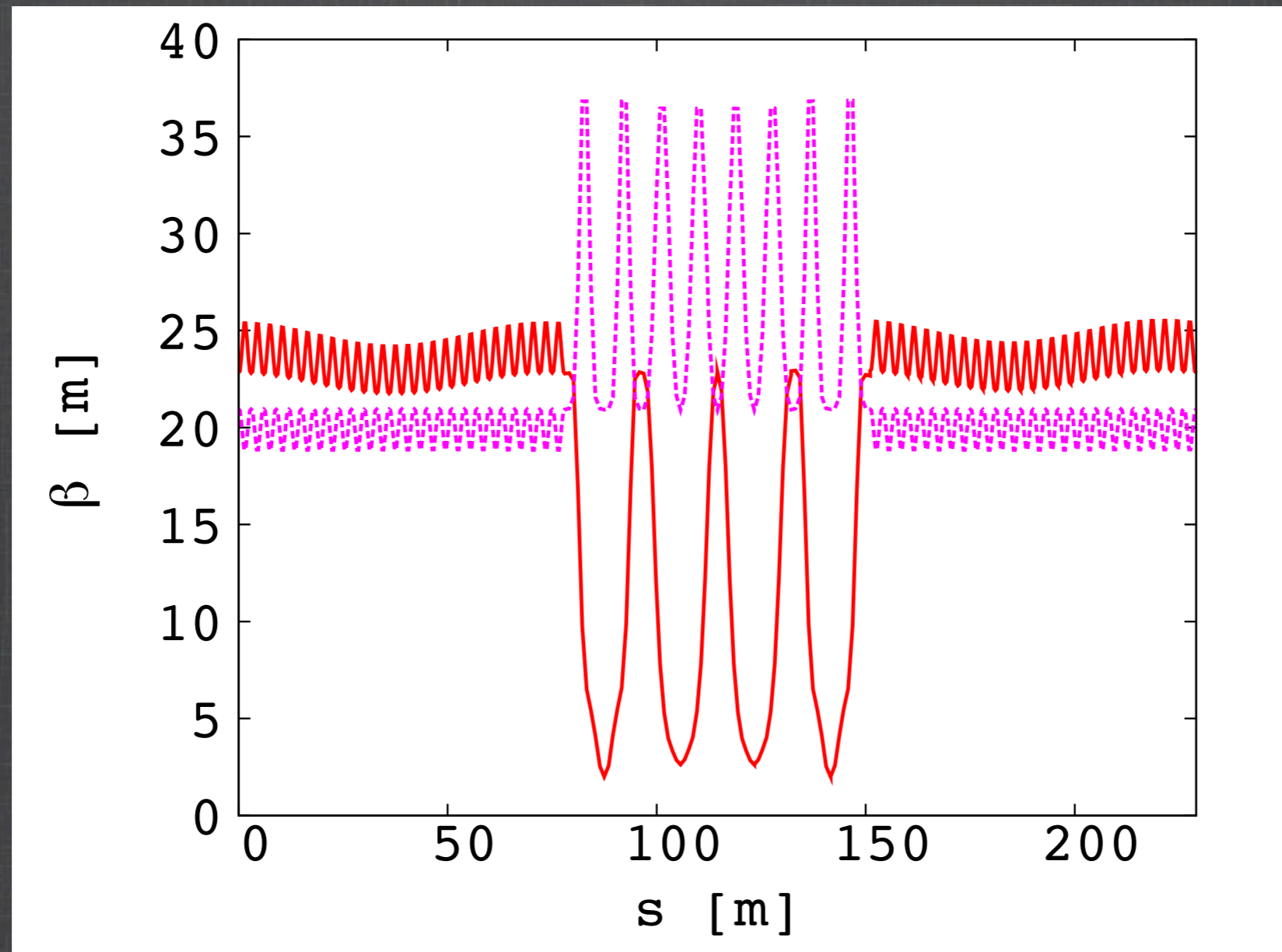
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Magnetic field for  $P_{\max}$  (+16%)



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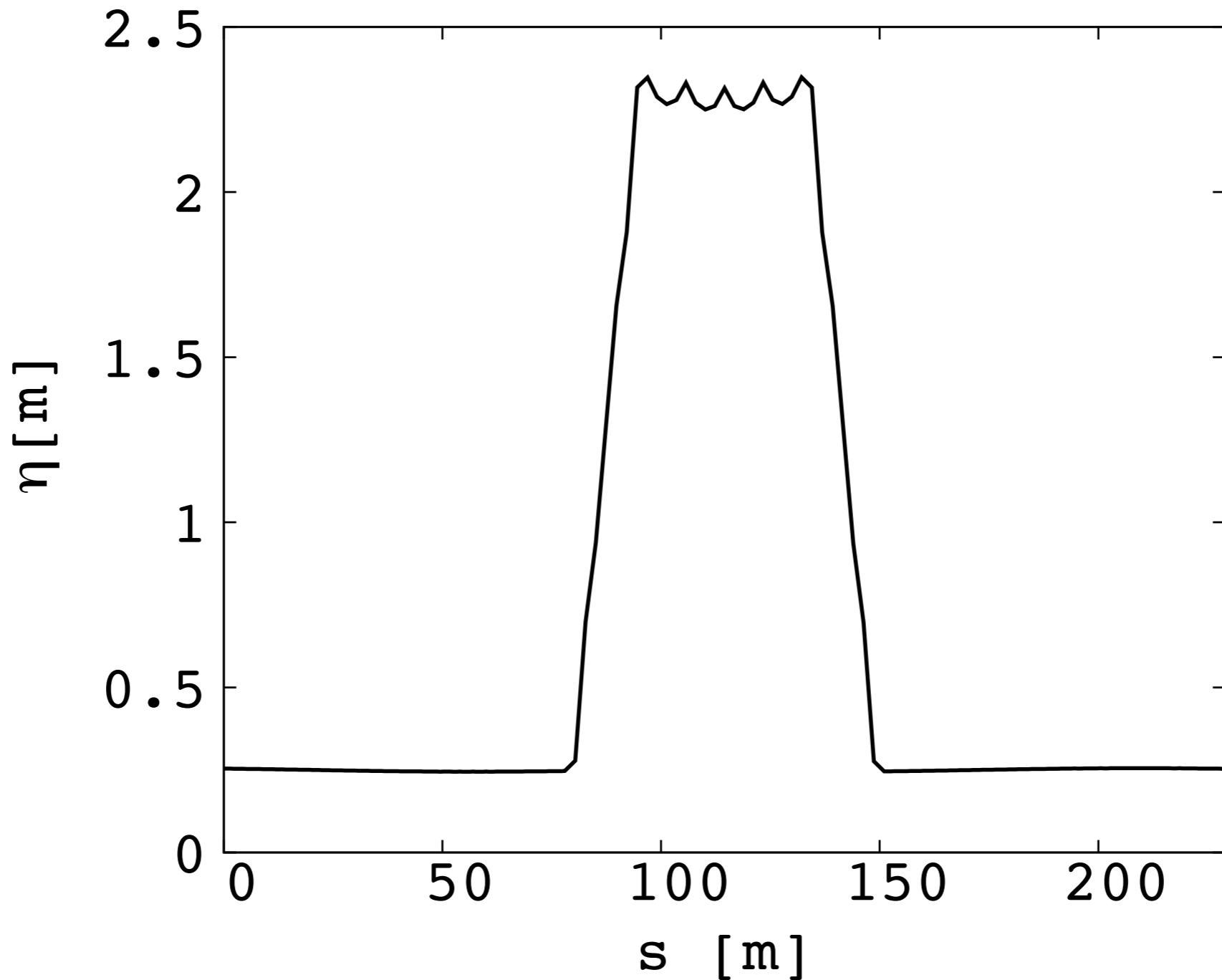
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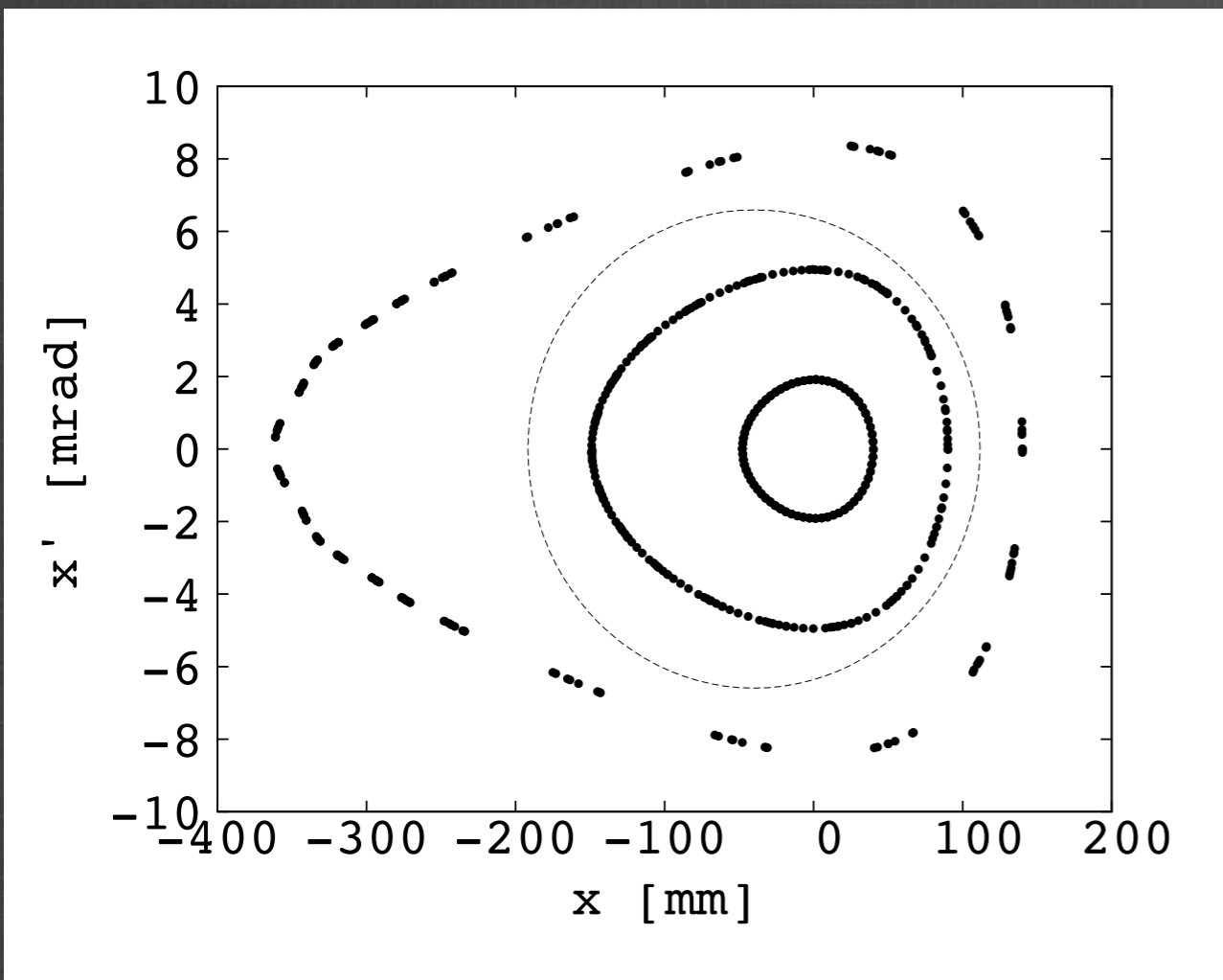
# OPTION #3

## Dispersion function at matching momentum

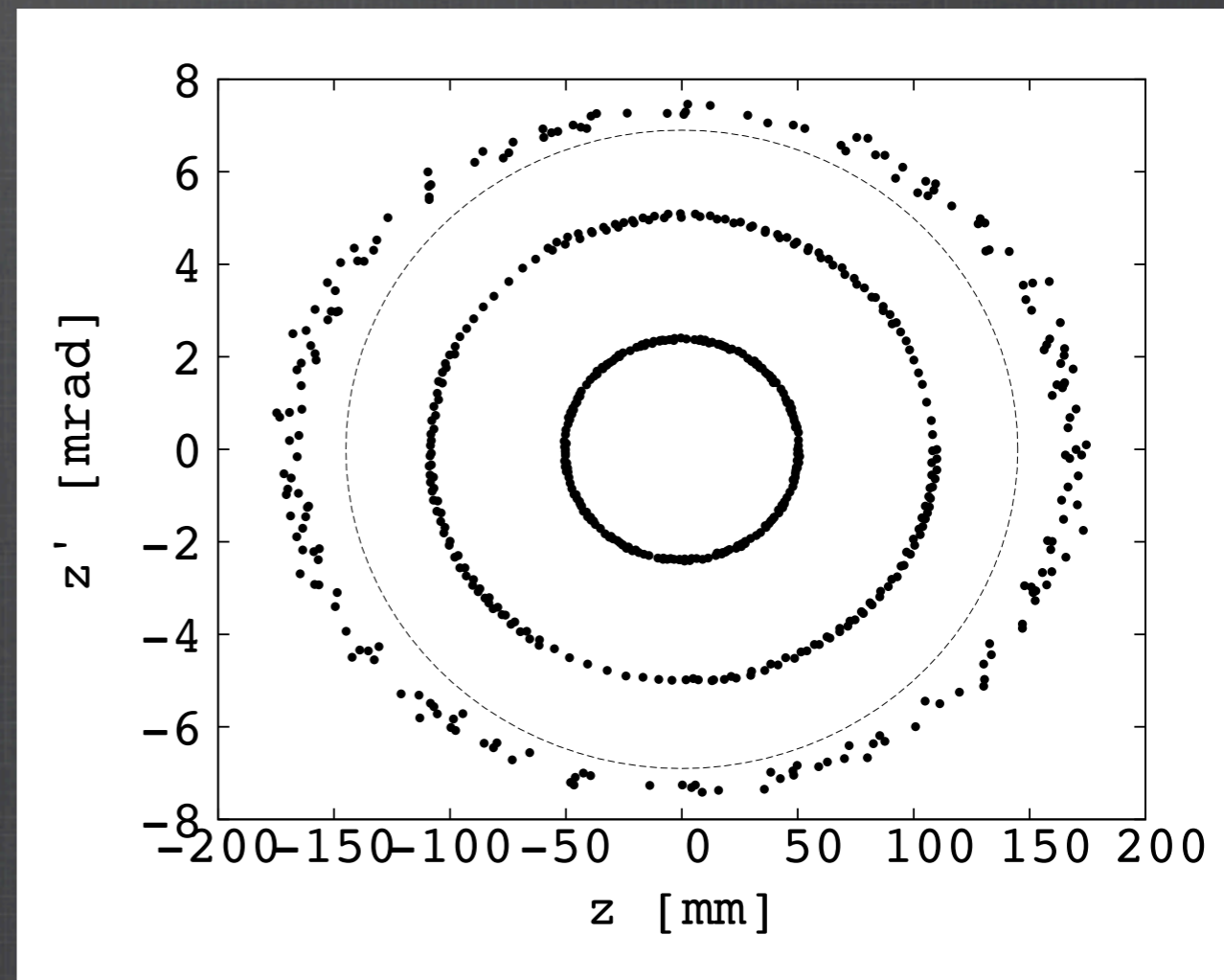


# OPTION #3

## Transverse acceptance



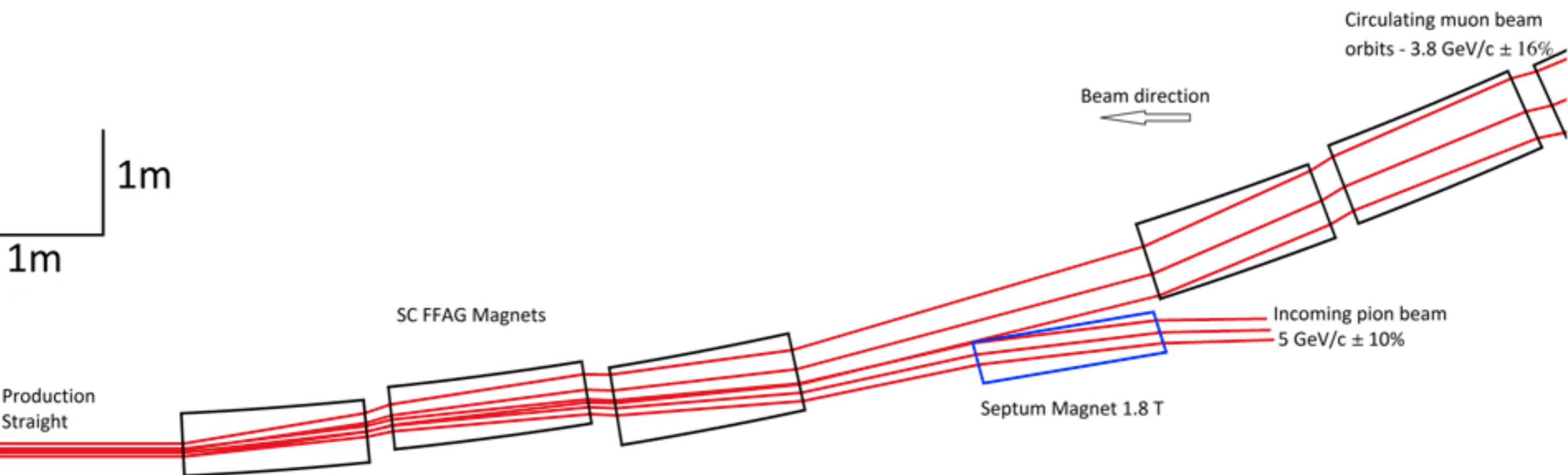
Maximum horizontal stable amplitude over 100 turns



Maximum vertical stable amplitude over 100 turns

# Stochastic Injection

## Preliminary results



Stochastic injection principle (J. Pasternak)



# Outline



- Zero-chromatic FFAG
- Racetrack FFAG muon decay ring
- Comparison





# Comparison



| Parameters   | FODO<br>(Jun. 2013) | RFFAG<br>"FODO-like" | RFFAG<br>"long" | RFFAG<br>"low-cost" |
|--|---------------------|----------------------|-----------------|---------------------|
| $L_{straight}$ [m]                                       | 185                 | 175                  | 230             | 156                 |
| Circumference [m]  | 480                 | 500                  | 613             | 460                 |
| Dynamical acceptance $A_{dyn}$                           | 0.6                 | 0.95                 | 0.95            | 0.95                |
| Momentum acceptance                                      | $\pm 10\%$          | $\pm 16\%$           | $\pm 16\%$      | $\pm 16\%$          |
| $\pi$ /POT within momentum acceptance                    | 0.094               | 0.171                | 0.171           | 0.171               |
| Fraction of $\pi$ decay in one straight ( $F_s$ )        | 0.48                | 0.47                 | 0.56            | 0.43                |
| Straight-circumference ratio ( $\Omega$ )                | 0.39                | 0.35                 | 0.38            | 0.34                |
| $A_{dyn} \times \pi/\text{POT} \times F_s \times \Omega$ | <b>0.011</b>        | <b>0.027</b>         | <b>0.035</b>    | <b>0.024</b>        |

# 4T magnet option

4T magnet (PAMELA type) would give several advantages:

- shrink the arc part of about 25 m,
- increase the straight / circumference ratio,
- better dispersion matching ( $\eta_{\max} < 2$  m),
- smaller excursion.



- Cheaper!
- Better performance!



# Summary





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- Promising results for racetrack FFAG ring as a muon decay ring for NuSTORM.



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- Cost may not be higher than FODO solution.

# Summary

- Promising results for racetrack FFAG ring as a muon decay ring for NuSTORM.
- Quite flexible regarding the circumference.
- Large 6D acceptance compared with FODO lattice.
- Cost may not be higher than FODO solution.
- Larger momentum acceptance ( $\pm 25\%$  achieved previously) for wider magnets.



**Thank you for your attention**





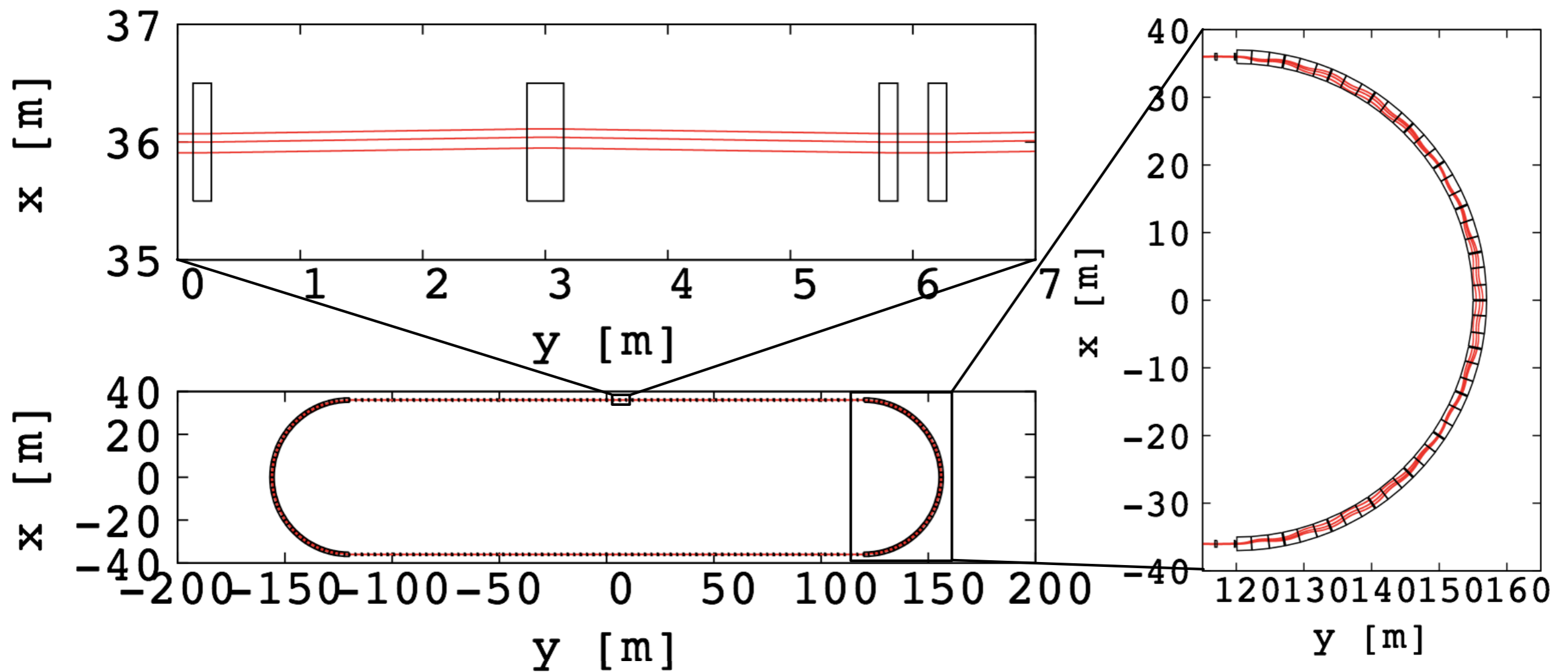
# Back-up slides



# Normal conducting arcs

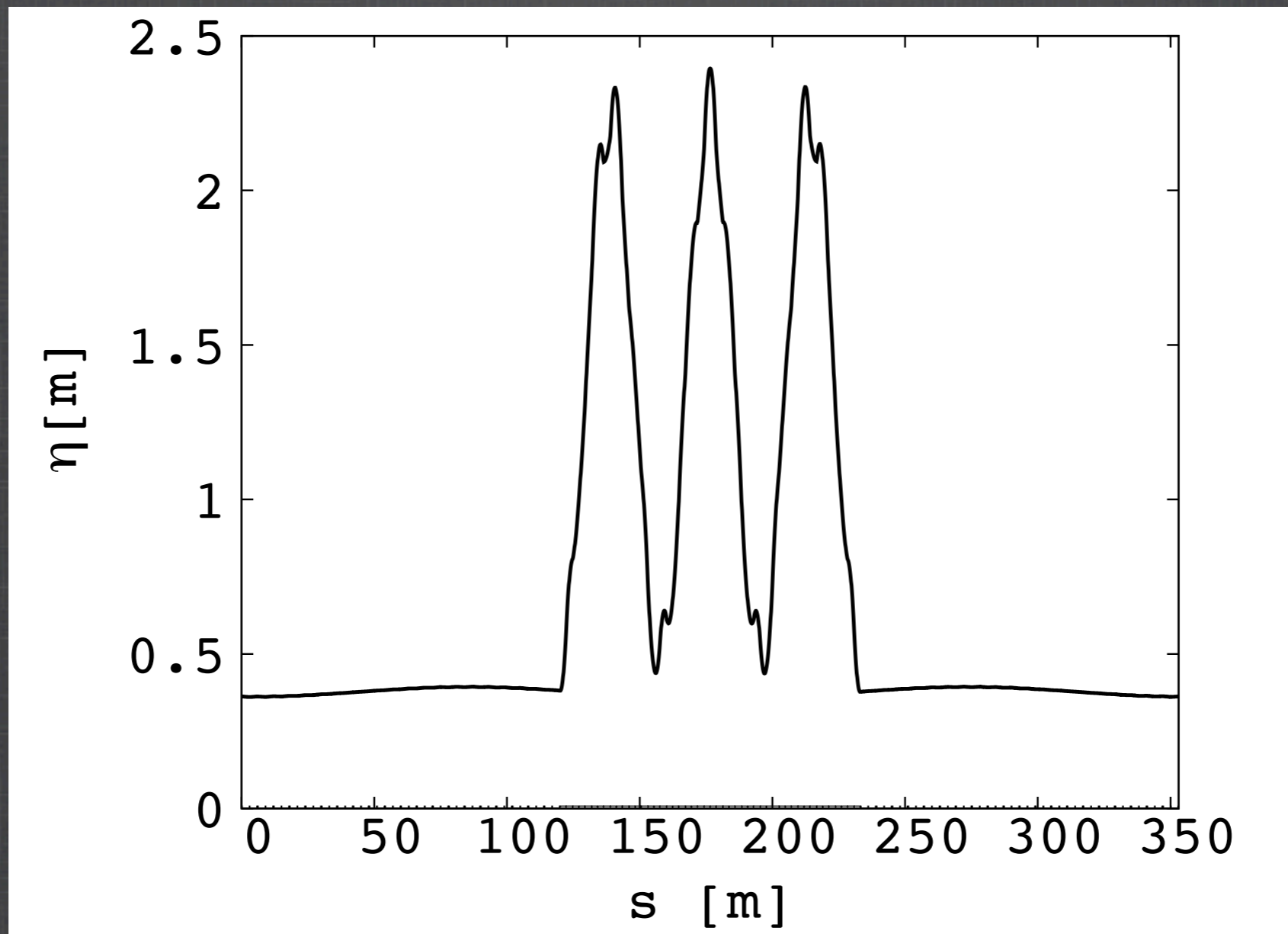


|   | Circular Section | Straight Section     |
|---|------------------|----------------------|
| Type  | FDF              | DFD                  |
| Cell radius [m]/opening angle [deg] or Length [m] | 36/11.25         | 6                    |
| k-value or m-value                                | 24.95            | 2.65 m <sup>-1</sup> |
| Packing factor                                    | 0.96             | 0.10                 |
| Horizontal phase advance /cell [deg]              | 67.5             | 13.1                 |
| Vertical phase advance /cell [deg]                | 11.25            | 16.7                 |
| Average dispersion /cell [m]                      | 1.39             | 0.38                 |
| Number of cells /ring                             | 16 × 2           | 40 × 2               |



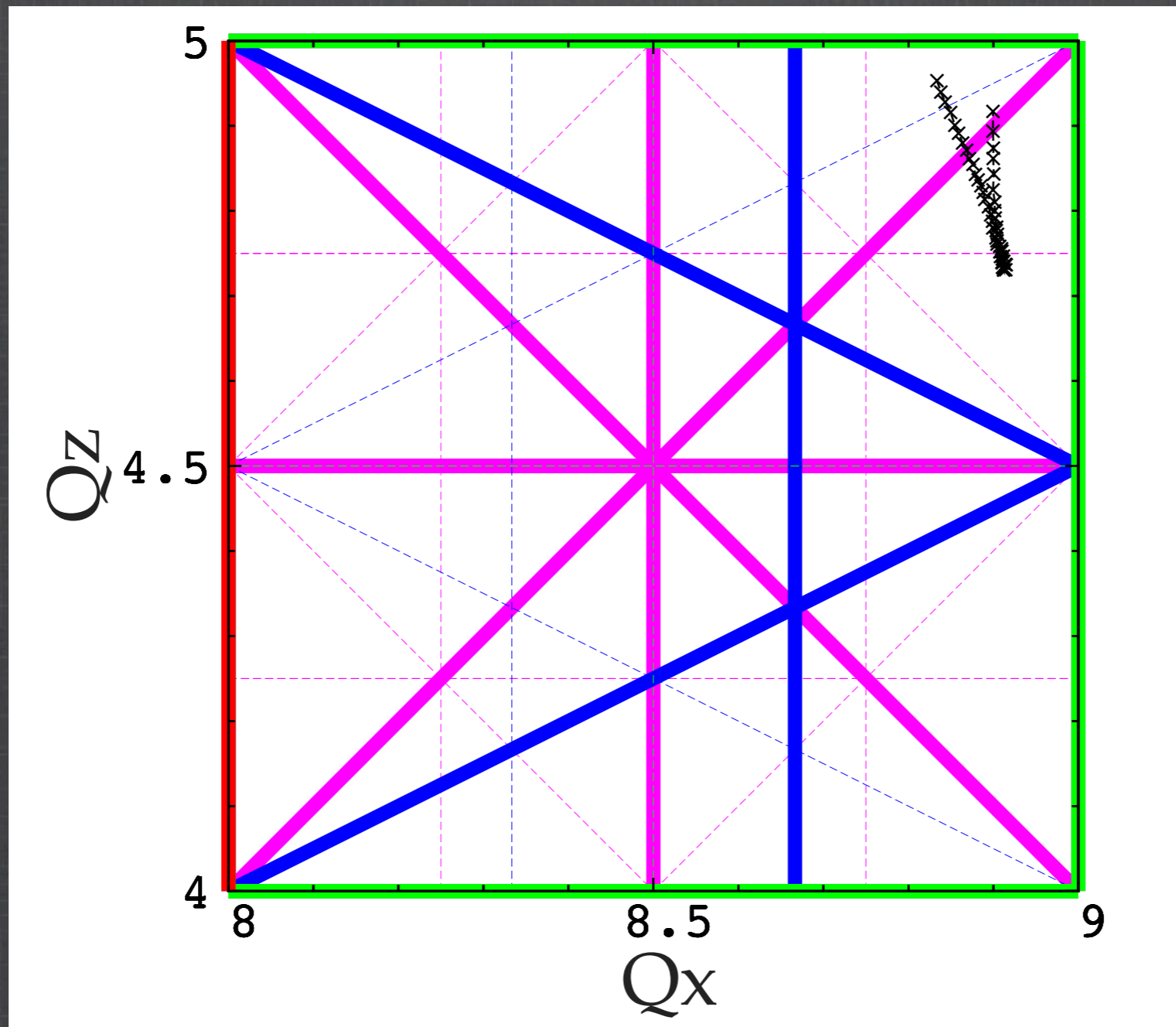
# Normal conducting arcs

Dispersion function



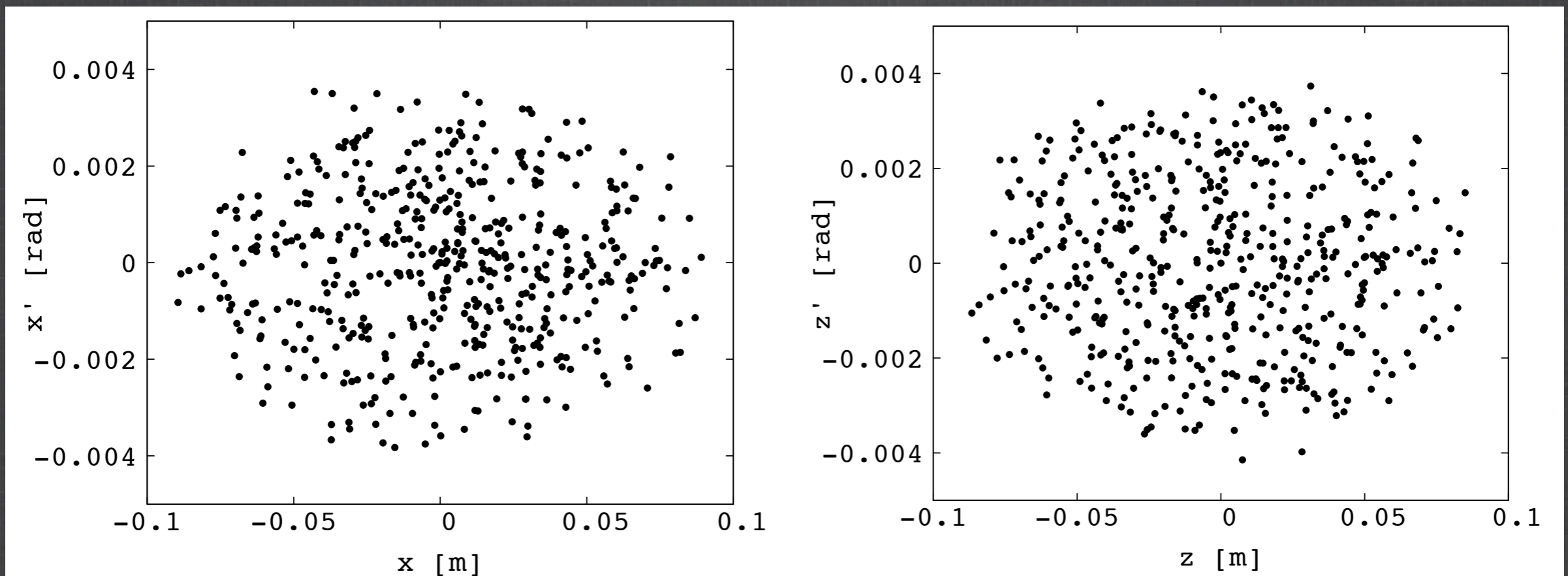
# Normal conducting arcs

Tune diagram  $\frac{\Delta P}{P} = \pm 26\%$



# Normal conducting arcs

Multi-particle tracking without dispersion matching.  
500 particles with a Waterbag distribution. Unnormalized emittances are  $400 \pi \text{ mm.mrad}$  in transverse planes.  
Momentum uniformly distributed around  $3.8 \text{ GeV}/c \pm 16\%$ .



Injected Beam in the horizontal (left) and vertical (right) phase spaces

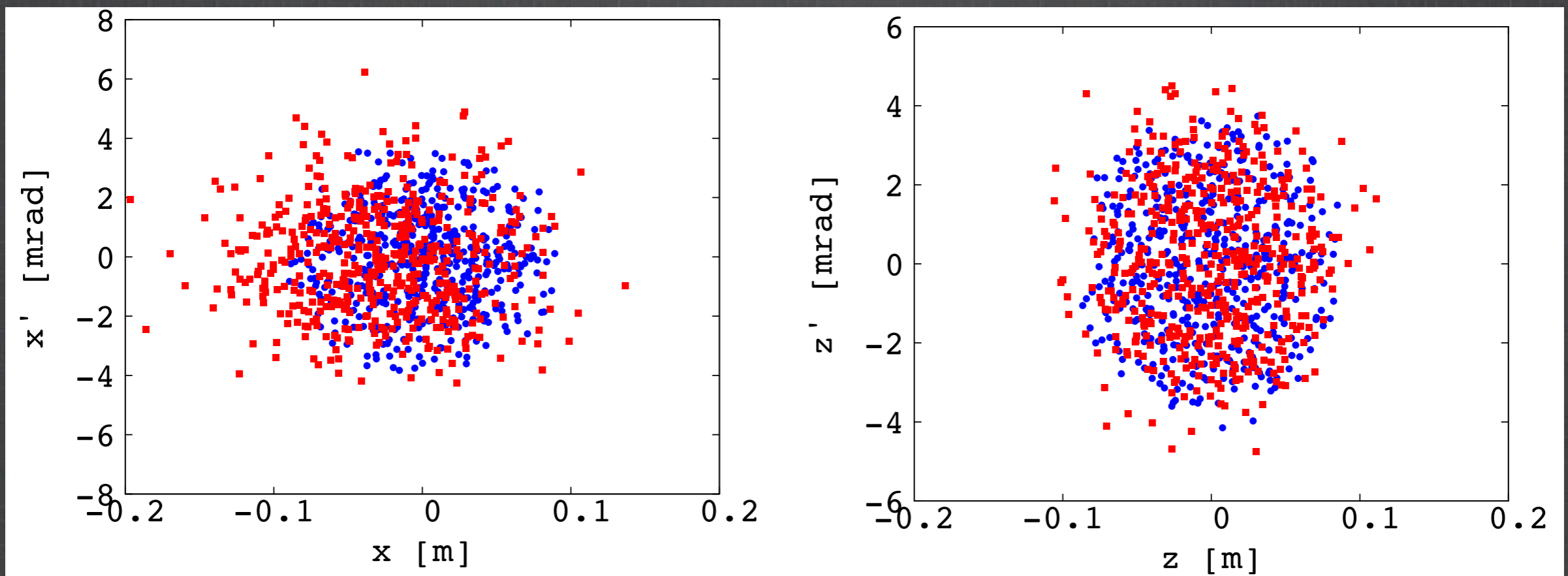


# Normal conducting arcs

Multi-particle tracking without dispersion matching.

After 60 turns  $\longrightarrow$  no particle lost.

(no muon decay implemented in the simulation).



Results in the horizontal (left) and vertical (right) phase spaces

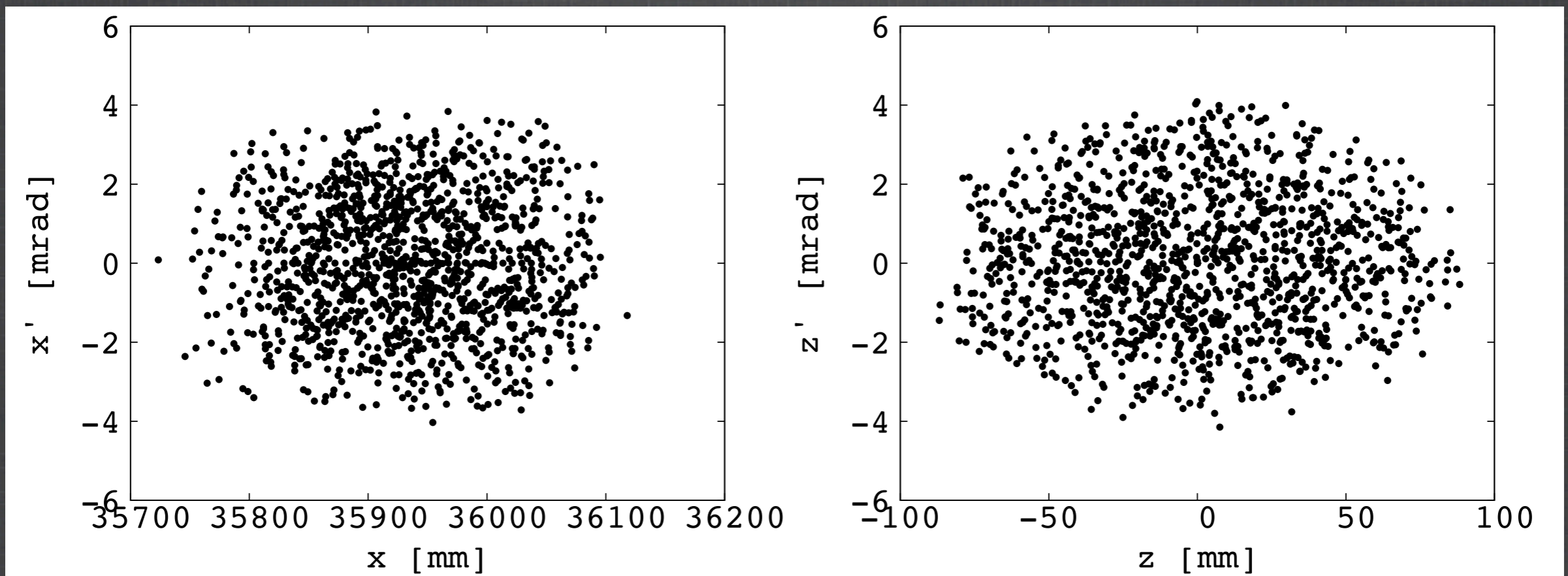
■ extraction  
● injection

# Normal conducting arcs

Multi-particle tracking with dispersion matching.

1350 particles with a Waterbag distribution. Unnormalized emittances are  $400 \pi \text{ mm.mrad}$  in transverse planes.

Momentum uniformly distributed around  $3.8 \text{ GeV}/c \pm 26\%$ .

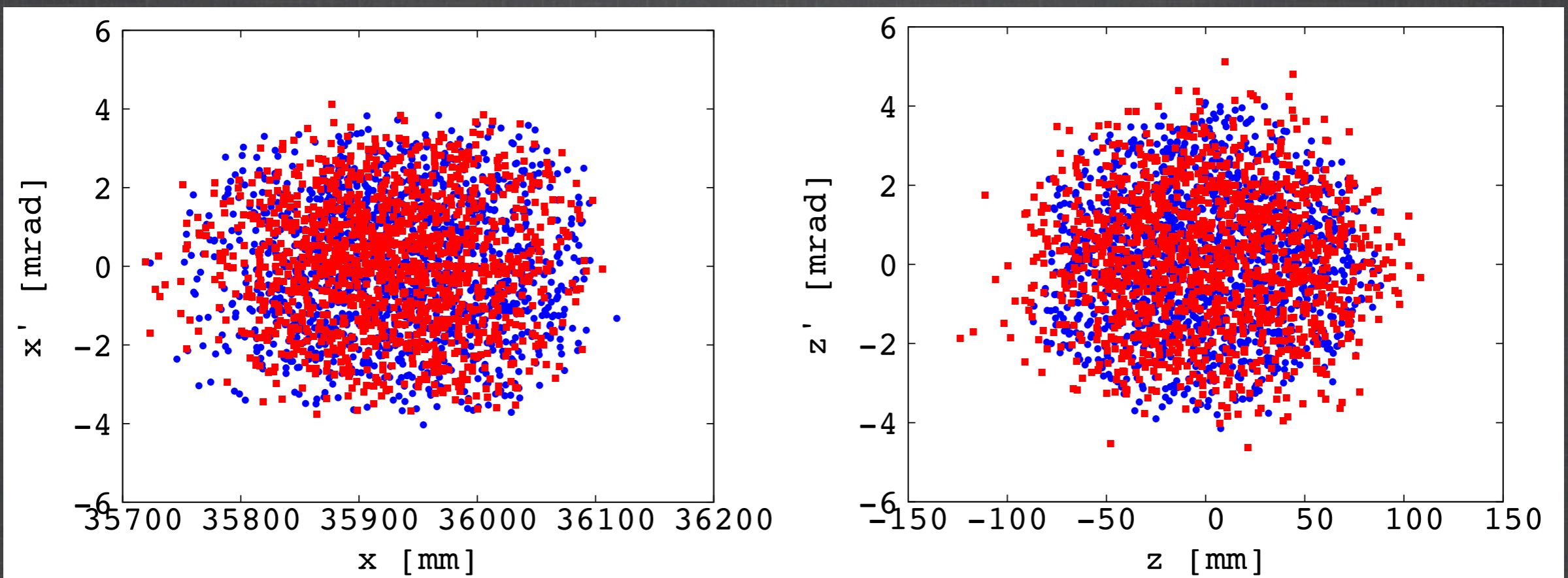


Injected Beam in the horizontal (left) and vertical (right) phase spaces

# Normal conducting arcs

Multi-particle tracking with dispersion matching.

After 60 turns  $\longrightarrow$  10 particles (0.7%) lost  
(no muon decay implemented in the simulation).



Results in the horizontal (left) and vertical (right) phase spaces

■ extraction  
● injection